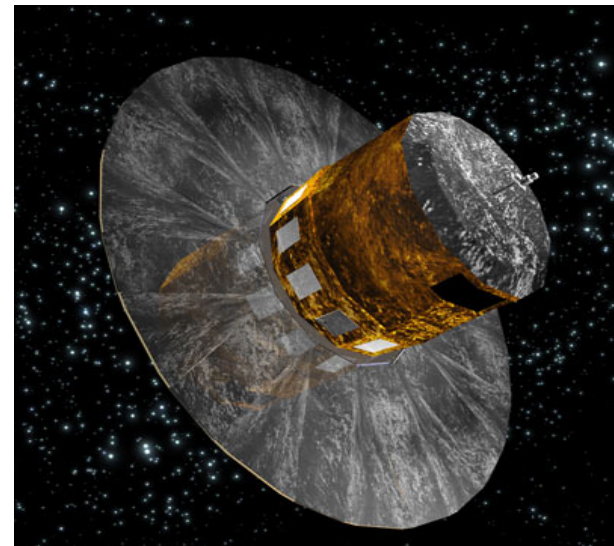
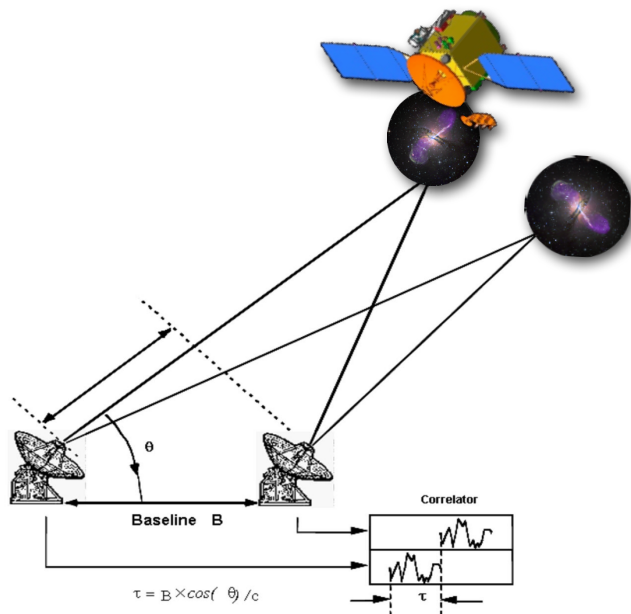


USNO, Washington D.C., 27 July 2017

# Comparing multiple Radio wavelength Celestial Frames and the Gaia Optical Frame



**Christopher S. Jacobs,** *Jet Propulsion Laboratory, California Institute of Technology*

A. De Witt, A. Bertarini, C. Garcia-Miro, D. Gordon, S. Horiuchi, J. Lovell, J. McCallum, M. Mercolino, J. Quick,  
L. Snedeker, G. Bourda, P. Charlot.



Max-Planck-Institut  
für Radioastronomie



HartRAO  
Hartebeesthoek Radio  
Astronomy Observatory



Isdefe



European Space Agency



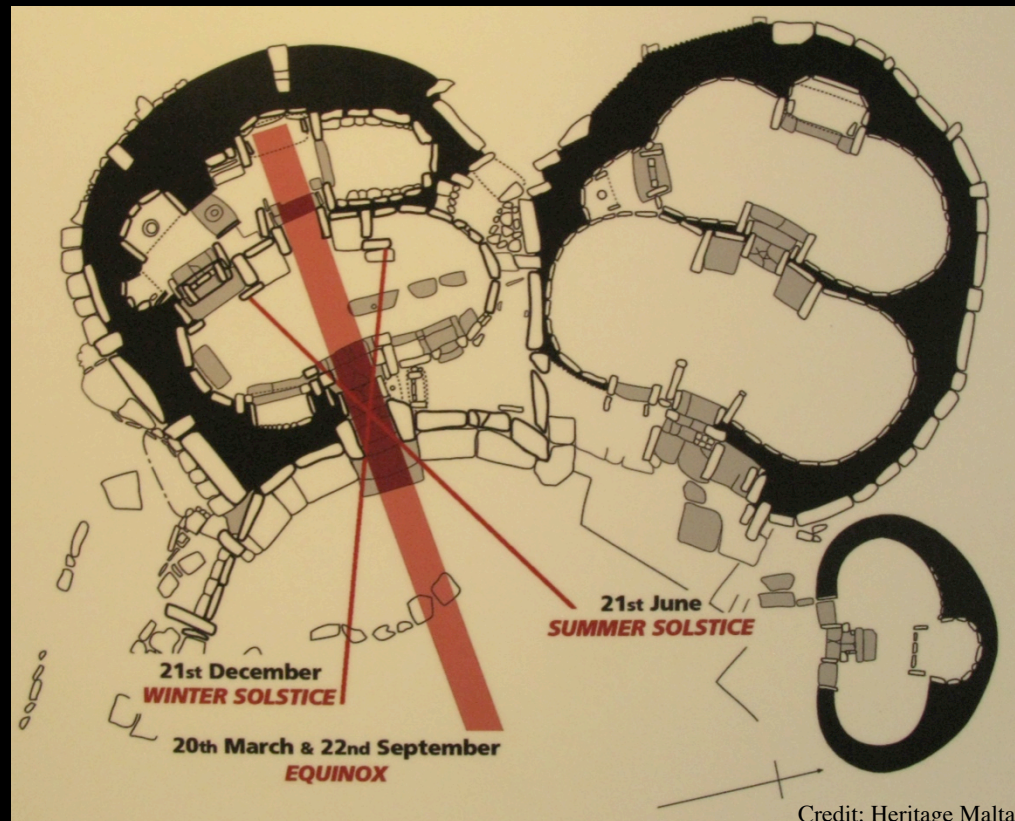
# Astrometry: measures positions in the sky, 5000+ years history!

Credit: Heritage Malta

Island of Malta  
Ggantija ~3500 B.C.  
Mnajdra ~3200 B.C.



Mnajdra solar alignments



Credit: Heritage Malta

Mnajdra,  
Malta



# Overview: Optical vs. Radio Celestial Frames

- Optical Frames: Used stars up through FK5 (Fricke+, 1988). Proper motions an issue. Hipparcos (Perryman+, 1997) had 100K stars mas precision but mas/yr PM precision. In late 1980s, early 1990s IAU started a move to quasars to leverage zero parallax & PM
- VLBI at SX (8 GHz, 3.6cm) has been only sub-mas frame until last 10 years  
(e.g. *Ma+*, *ICRF1*, 1998, *Ma+*, *ICRF2*, 2009)
- K-band (24 GHz, 1.2cm) now sub-mas (*Lanyi+*, 2010; *de Witt+*, 2016, 2017)
- X/Ka (32 GHz, 9mm) also sub-mas (*Jacobs+*, 2016, 2017)
- Gaia optical: data release #1 is sub-mas for auxiliary quasar solution (*Prusti+*, 2017)
- Precision is excellent allowing 3-D rotational alignment precision of 10 to 20  $\mu$ as
- Accuracy limited by VLBI systematics due to weak southern geometry, troposphere, etc. at few 100  $\mu$ as
- Gaia precision limited to  $\sim 500$   $\mu$ as by short span of data in DR#1.



# What objects can we use?



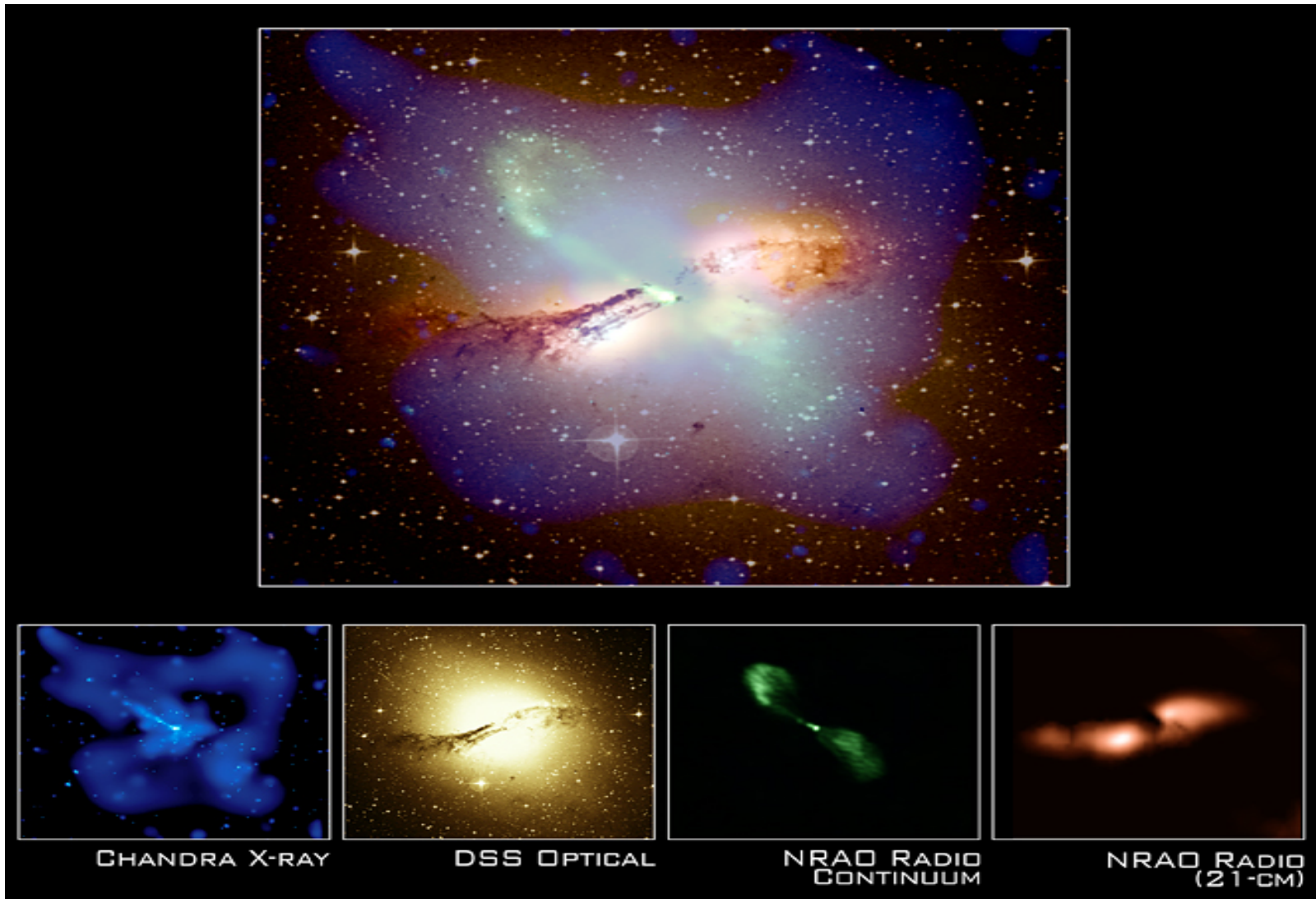
## Methods for Tying Optical and Radio Celestial Frames

- Need common objects well measured in both optical and radio
- **Radio stars:** Previous generation used galactic stars that emit in radio,  
**Crude by today's standards: difficult to achieve desired accuracy level.**  
e.g. Lestrade et al. (1995) used radio stars to tie Hiparcos & VLBI.
- **Thermal emission from regular stars:**  
350 GHz astrometry using Atacama Large Millimeter Array (ALMA)  
Fomalont et al. (pilot observations)  
Verifies bright end of optical, **but likely limited to 500 – 1000  $\mu$ as (2.5 to 5 ppb).**
- **Extra-galactic Quasars:** detectable in both radio and optical  
potential for better than 100  $\mu$ as to 20  $\mu$ as (0.5 to 0.1 ppb).  
**Strengths: extreme distances (> 1 billion light years) means no parallax or proper motion**



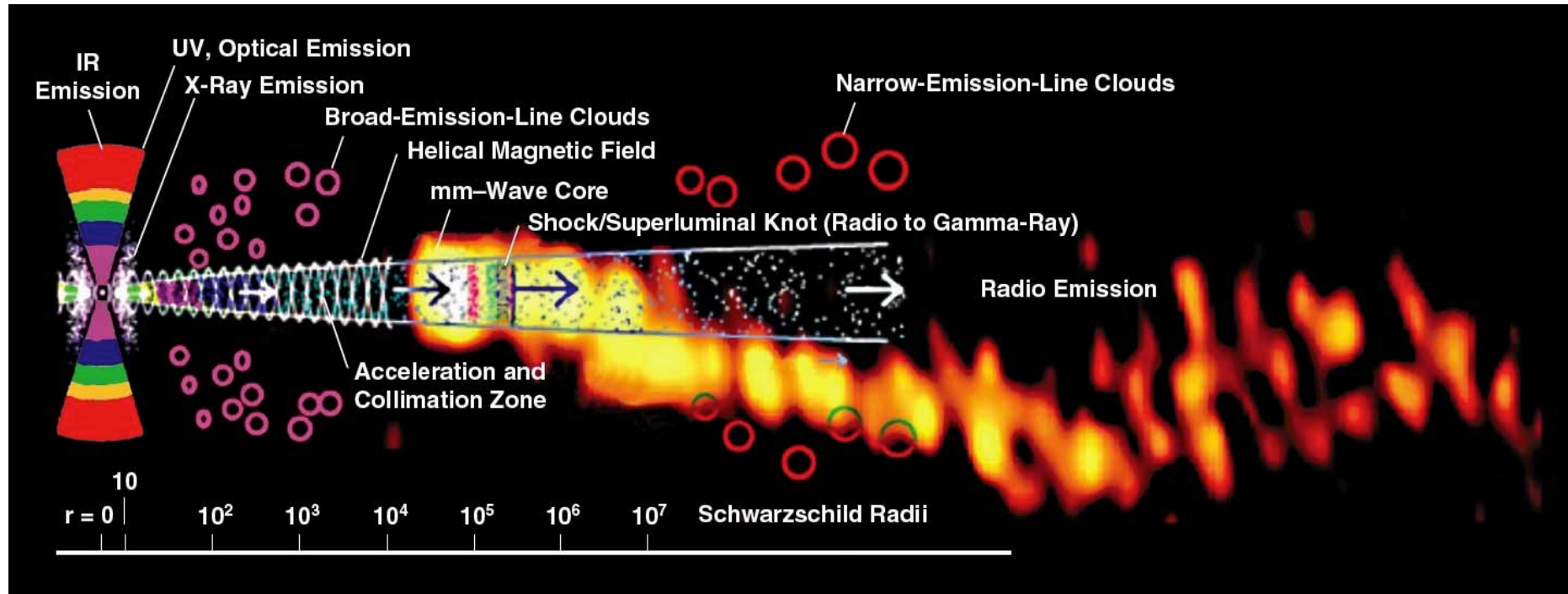
# The Source Objects

# Example Extragalactic Source: Centaurus-A in X-ray, Optical, Radio



Credits: X-ray (NASA/CXC/M. Karovska et al.); Radio 21-cm image (NRAO/VLA/Schiminovich, et al.),  
Radio continuum image (NRAO/VLA/J. Condon et al.); Optical (Digitized Sky Survey U.K. Schmidt Image/STScI)

# Active Galactic Nuclei (*Marscher*)



$R \sim 0.1 - 1 \mu\text{as}$

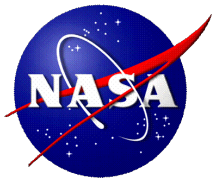
$1 \text{ mas}$

Features of AGN: *Note the Logarithmic length scale.*

“Shock waves are frequency stratified, with highest synchrotron frequencies emitted only close to the shock front where electrons are energized. The part of the jet interior to the mm-wave core is opaque at cm wavelengths. At this point, it is not clear whether substantial emission occurs between the base of the jet and the mm-wave core.”

*Credits: Alan Marscher, 'Relativistic Jets in Active Galactic Nuclei and their relationship to the Central Engine,' Proc. of Science, VI Microquasar Workshop: Microquasars & Beyond, Societa del Casino, Como, Italy, 18-22 Sep 2006. Overlay (not to scale): 3 mm radio image of the blazar 3C454.3 (Krichbaum et al. 1999)*

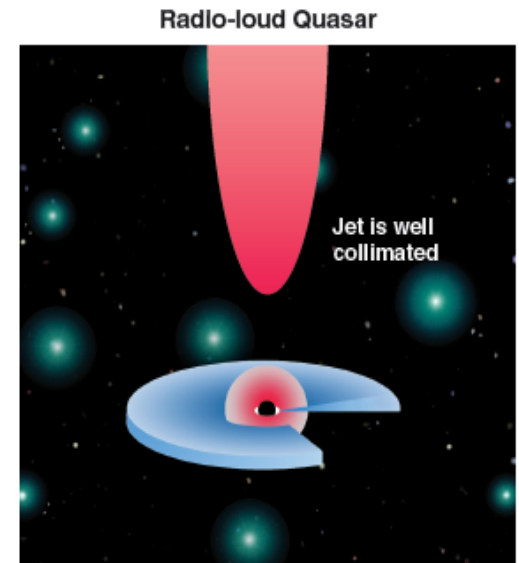
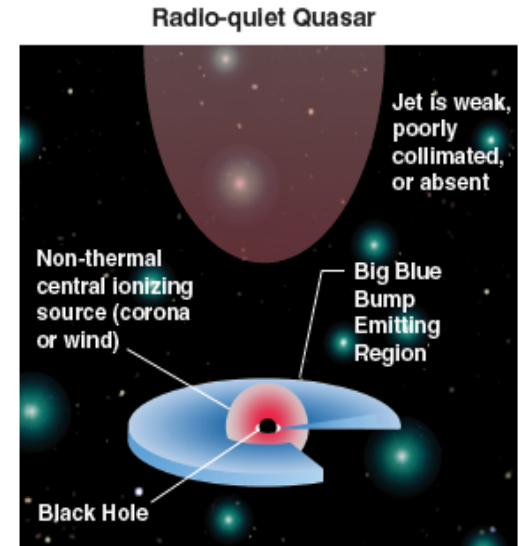




# Optical vs. Radio positions

Positions differences from:

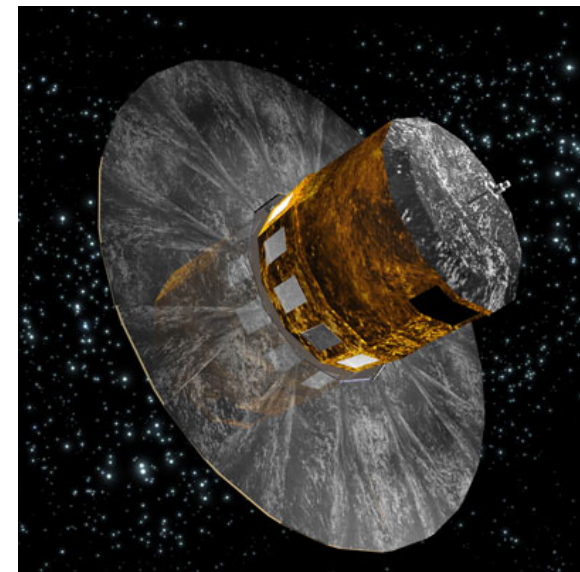
- Astrophysics of emission centroids
  - radio: synchrotron from jet
  - optical: synchrotron from jet?  
non-thermal ionization from corona?  
big blue bump from accretion disk?
- Instrumental errors both radio & optical
- Analysis errors



# The Gaia Optical Frame

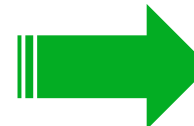
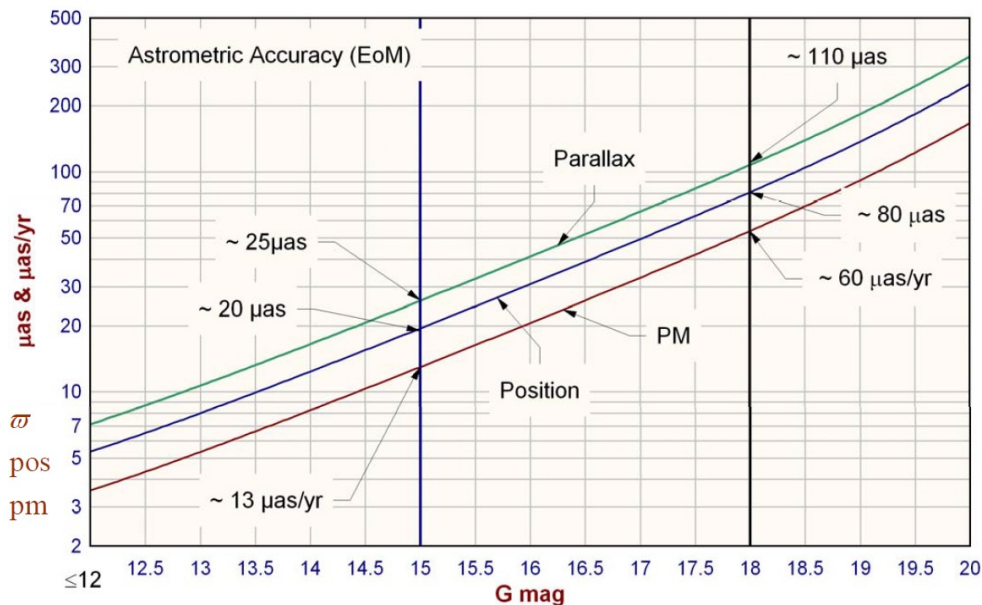
# ESA's Gaia optical Astrometry

- Method: extremely accurate centroid of 60 mas pixels. Compare to VLBI sub-mas beam.
- **Astrometry & photometric survey to  $V = 20.7^{\text{mag}}$** 
  - $\sim 10^9$  objects: stars, QSOs, solar system, galaxies.
- **Gaia Celestial Reference Frame (GCRF):**
  - Optically bright objects ( $V < 18^{\text{mag}}$ ) give best precision
  - 1st release Gaia astrometric catalog DR1 Sep 2016,
  - DR2 Apr 2018.



Credit: F. Mignard (2013)

## Anticipated precision of Gaia catalogue



## Gaia Data Release-1:

**$\sim 0.3$  mas in positions and parallaxes for 2 million brightest stars**

**$\sim 10$  mas for rest of the stars**

**$\sim 0.5$  mas for ICRF2 quasars (auxiliary solution)**



Celestial Frames  
using  
Radio Interferometry  
(VLBI)

# Radio Interferometry: Long distance phased arrays

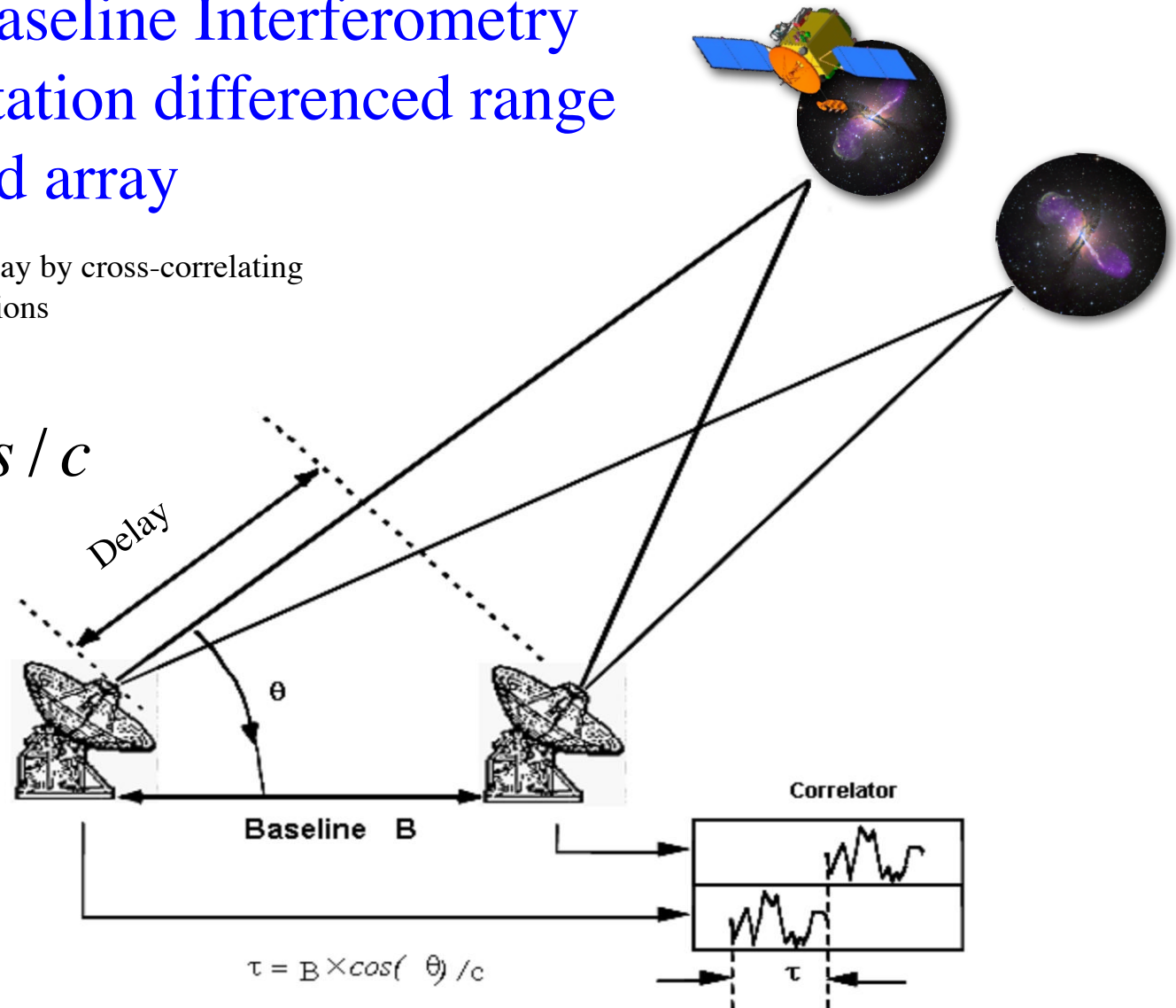
## Very Long Baseline Interferometry is a type of station differenced range from a phased array

- Measures geometric delay by cross-correlating signal from two (2) stations

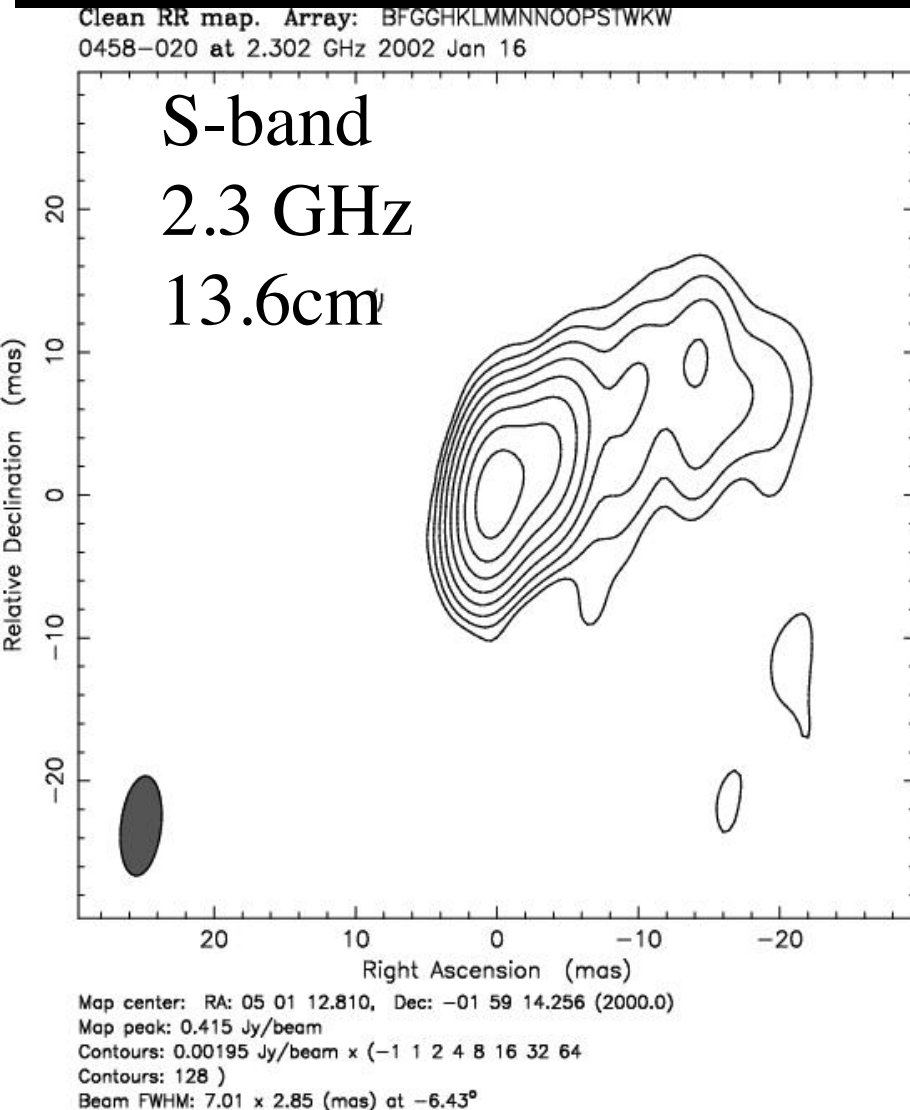
$$\tau = B \cdot s / c$$

10,000 km baselines  
give resolution of  
 $\lambda/B \sim$  few nanoradian  
sub-mas beam !!

Resolves away all  
but galactic nucleus



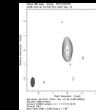
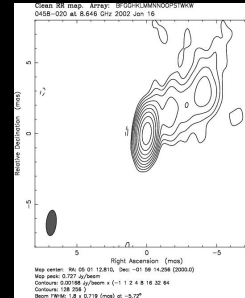
# Radio Source Structure vs. Frequency



**X-band**  
**8.6 GHz**  
**3.6cm**

**K-band**  
**24 GHz**  
**1.2cm**

**Q-band**  
**43 GHz**  
**0.7cm**



**The sources**  
**become better →**  
**Less structure**

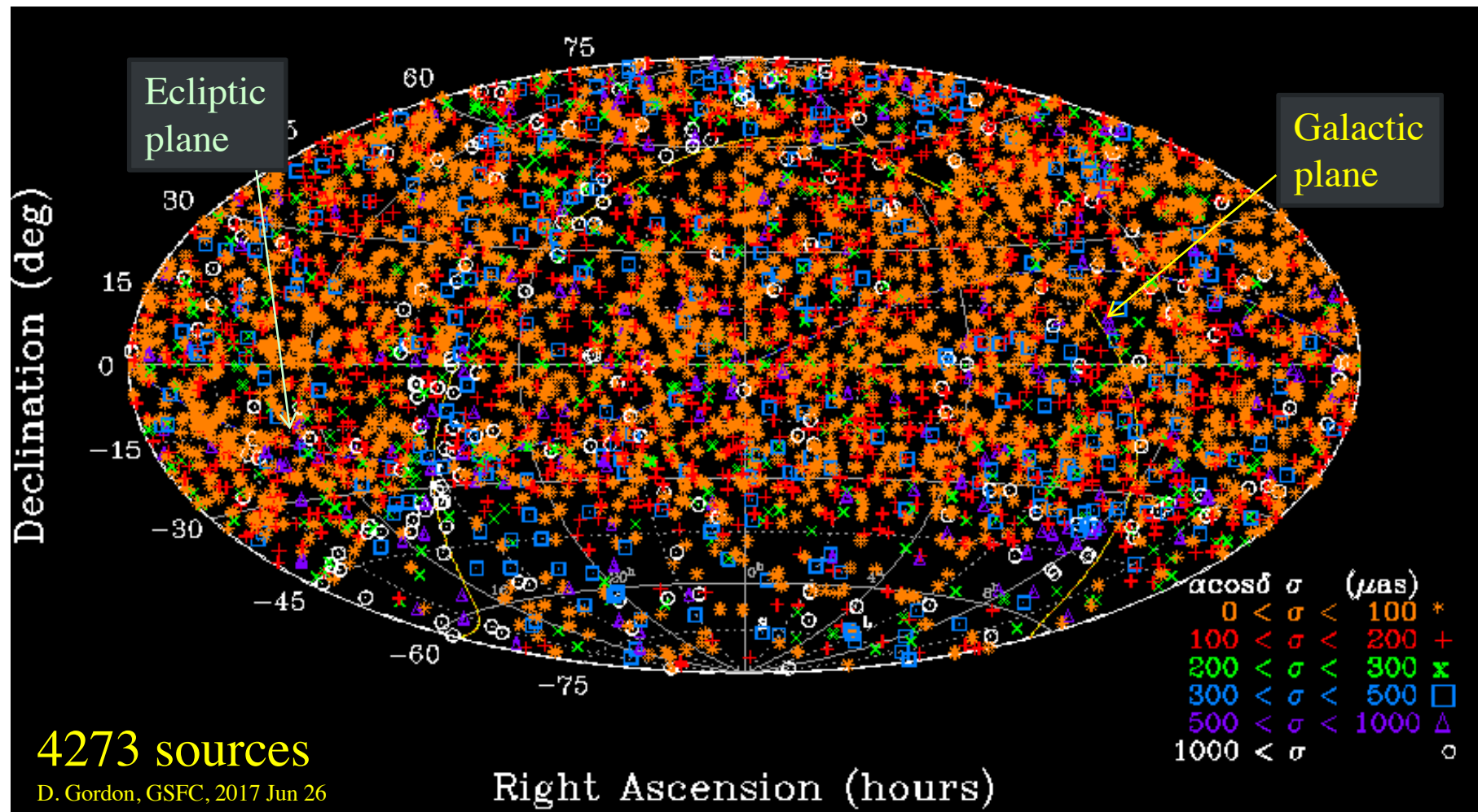
**Ka-band**  
**32 GHz**  
**0.9cm**

Images credit: Pushkarev & Kovalev A&A, 544, 2012 (SX);

Charlot et al, AJ, 139, 2010 (KQ)

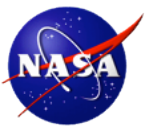


# SX (8.4 GHz, 3.6cm) *VLBA*+~ 100 other IVS

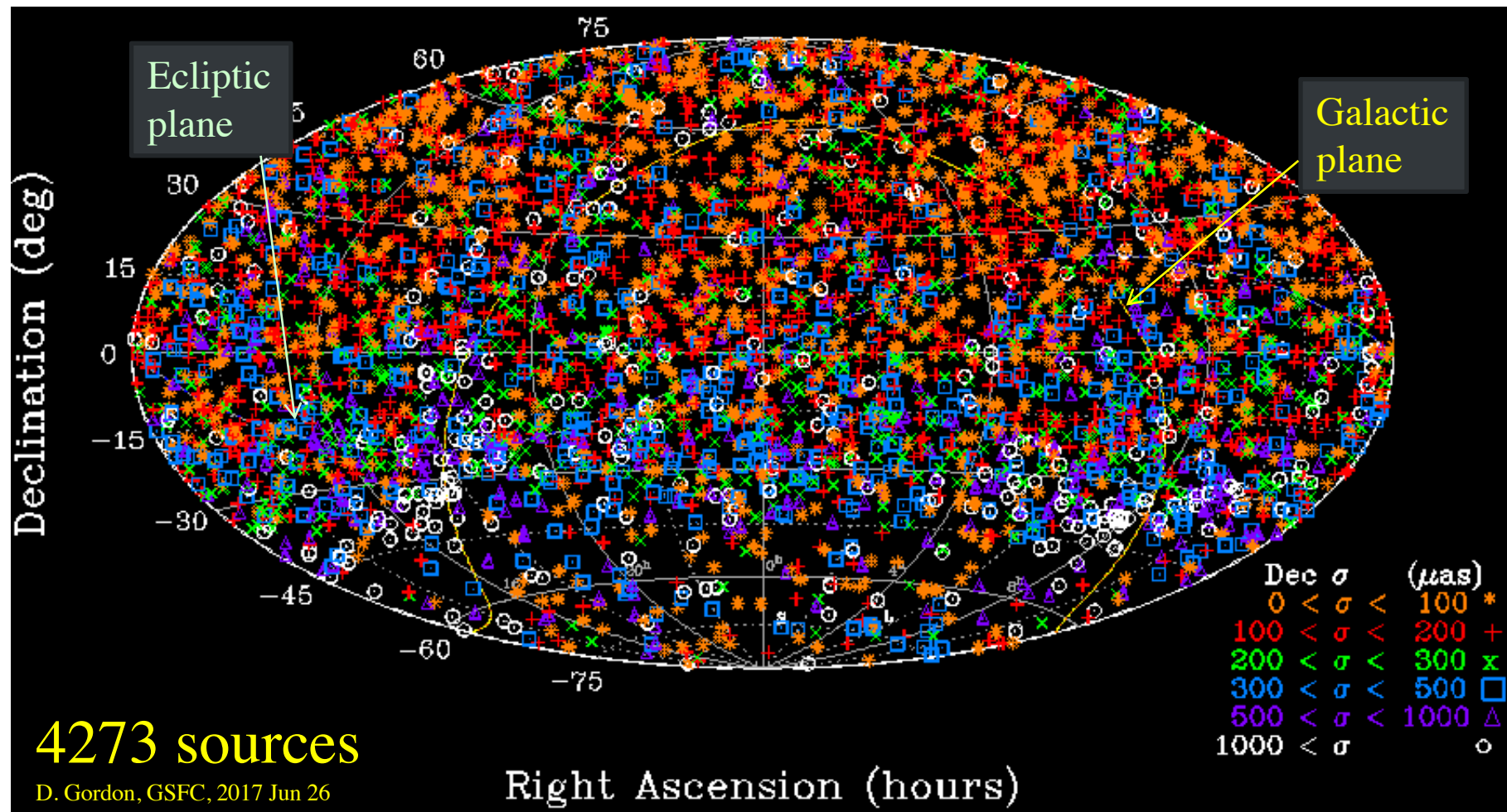


- **Strengths:**
  - 4273 sources
  - Excellent coverage North of  $\delta -30$  deg
  - median precision  $< 50 \mu\text{as}$
  - SX's 12 million observations, 40 years
  - over 100 stations contributed

- **Weaknesses:**
  - Poor coverage south of  $\delta -40$  deg
  - only 20% of sources in  $> 10$  sessions
  - source structure worse than K or XKa.

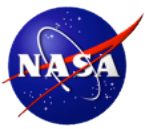


# SX (8.4 GHz, 3.6cm): Dec precision weaker than RA

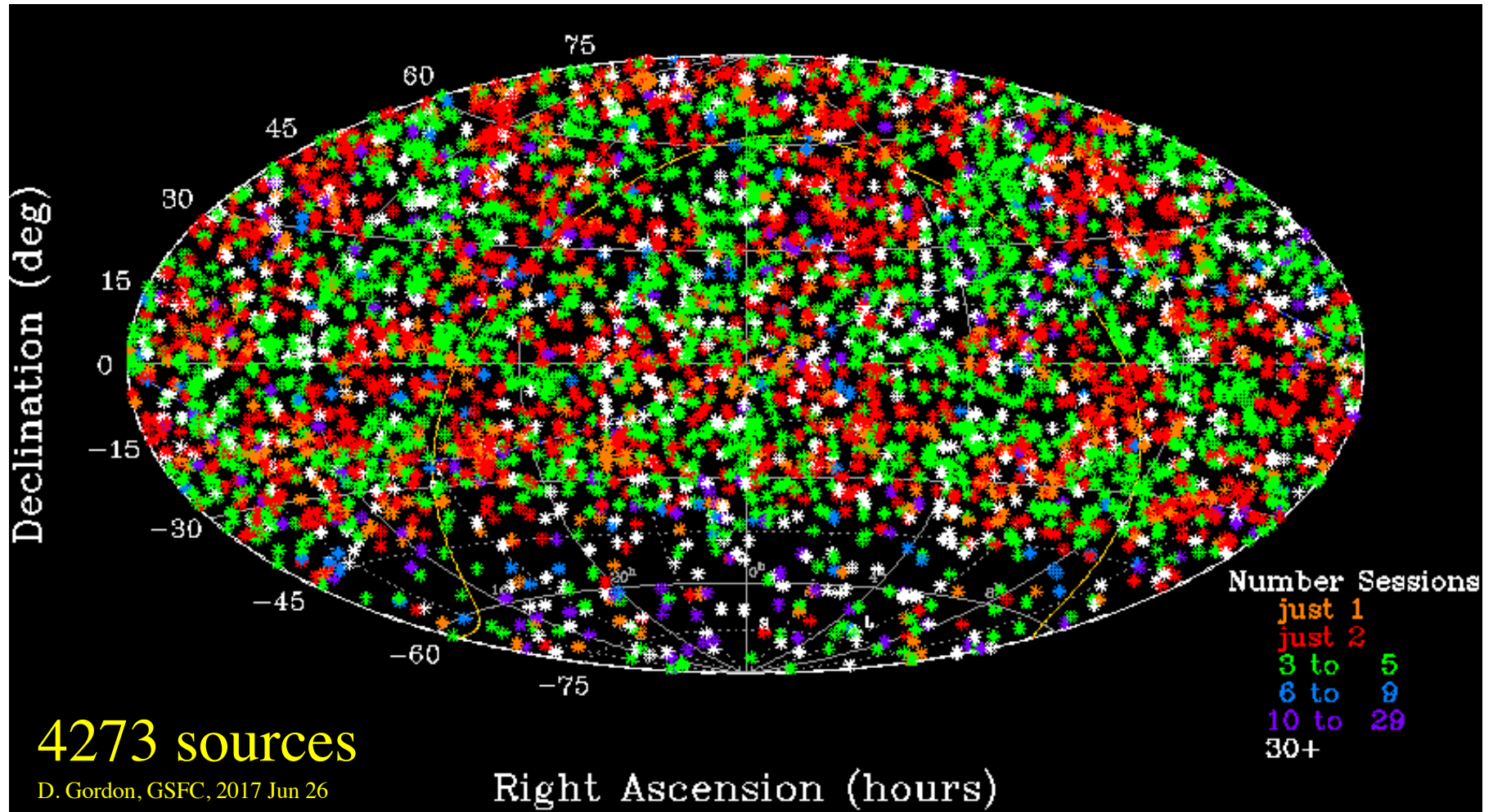


- **Strengths:**
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  - Excellent coverage North of  $\delta$  -30 deg
  - median precision  $< 50 \mu\text{as}$
  - SX's 12 million observations, 40 years
  - over 100 stations contributed

- **Weaknesses:**
  - Poor coverage south of  $\delta$  -40 deg
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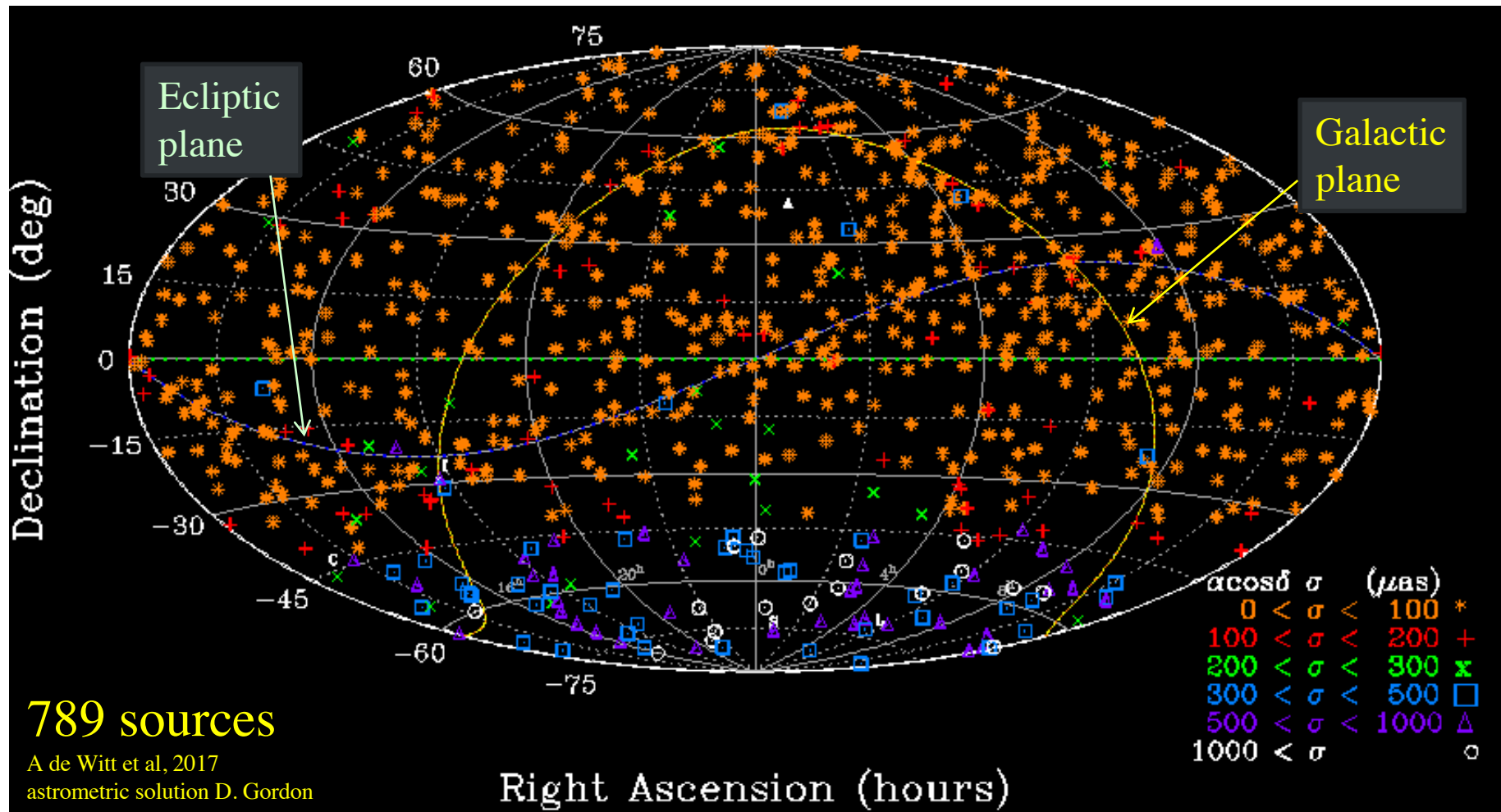


SX: Number Sessions,  $\sim 800 > 10$  sessions, rest 2-5 survey sessions



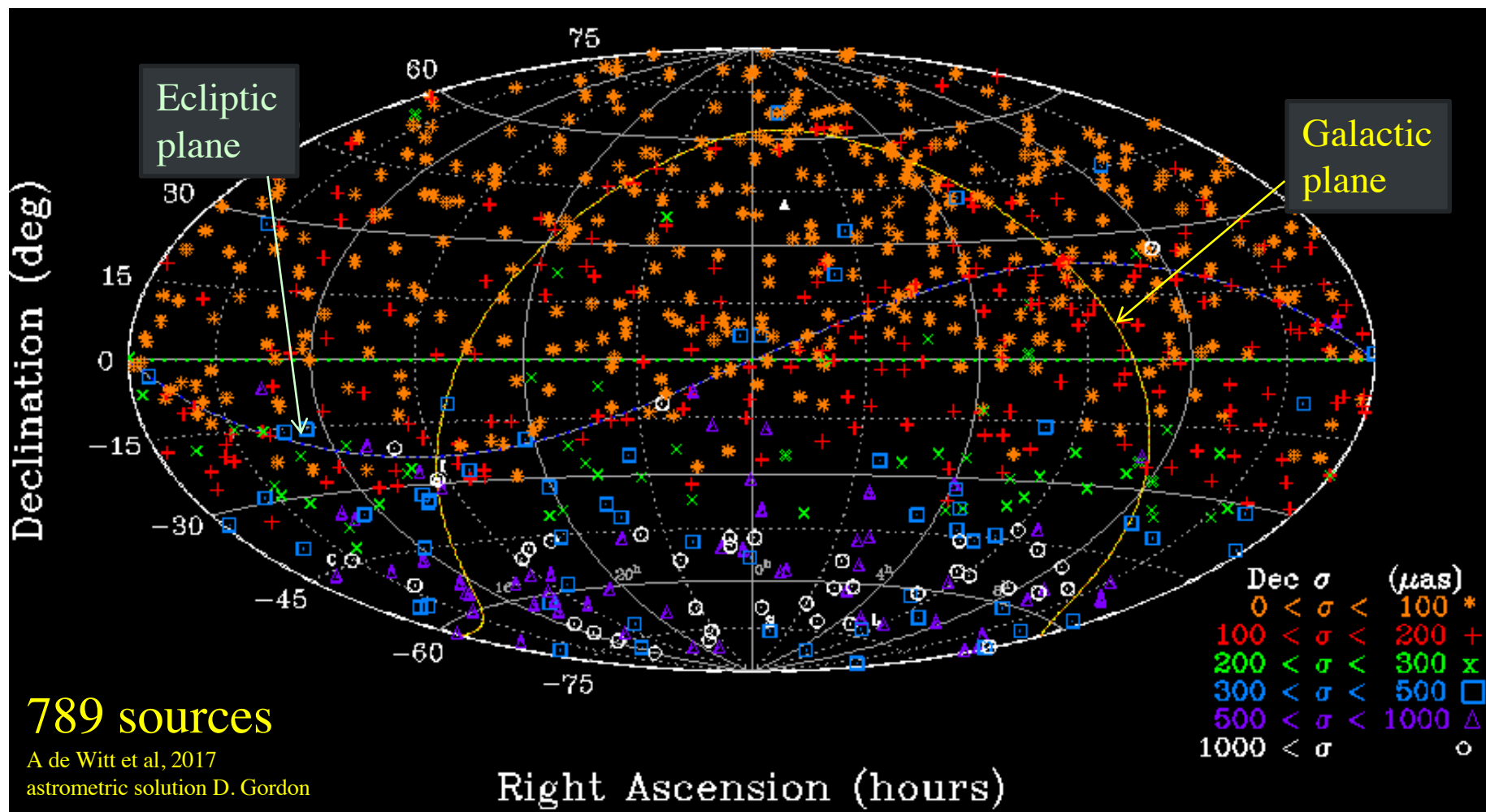
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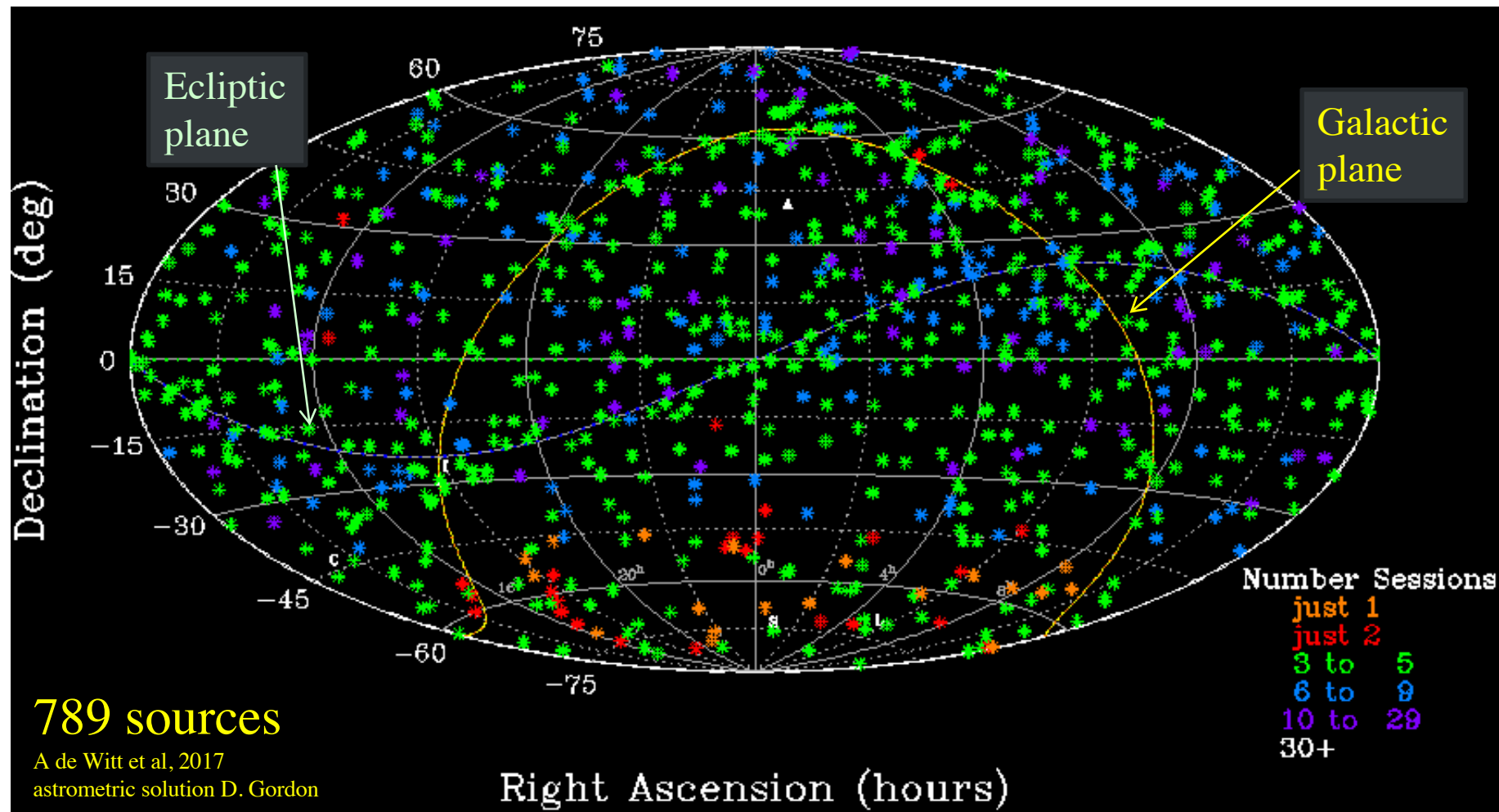
- **Strengths:**
  - Uniform spatial density
  - Galactic plane sources (Petrov+ 2006)
  - less structure than S/X (3.6cm)
  - precision  $< 100 \mu\text{as}$
  - needed  $\sim 0.25$  million observations vs. SX's 12 million!

- **Weaknesses:**
  - Ionosphere only partially calibrated by GPS.
  - No solar plasma calibrations
  - South ( $\delta < -30$  deg) weak due to limited HartRAO, South Africa to Hobart, Tasmania data



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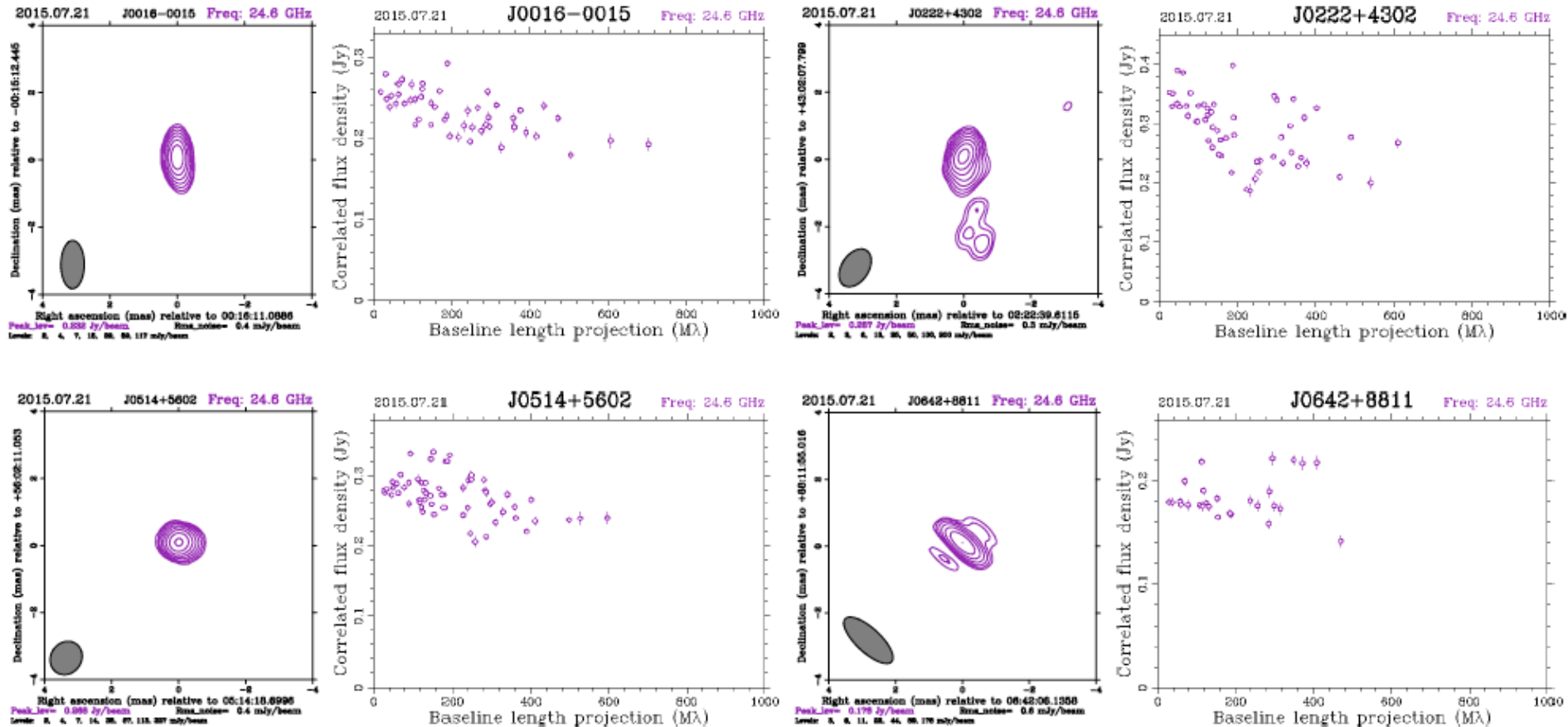
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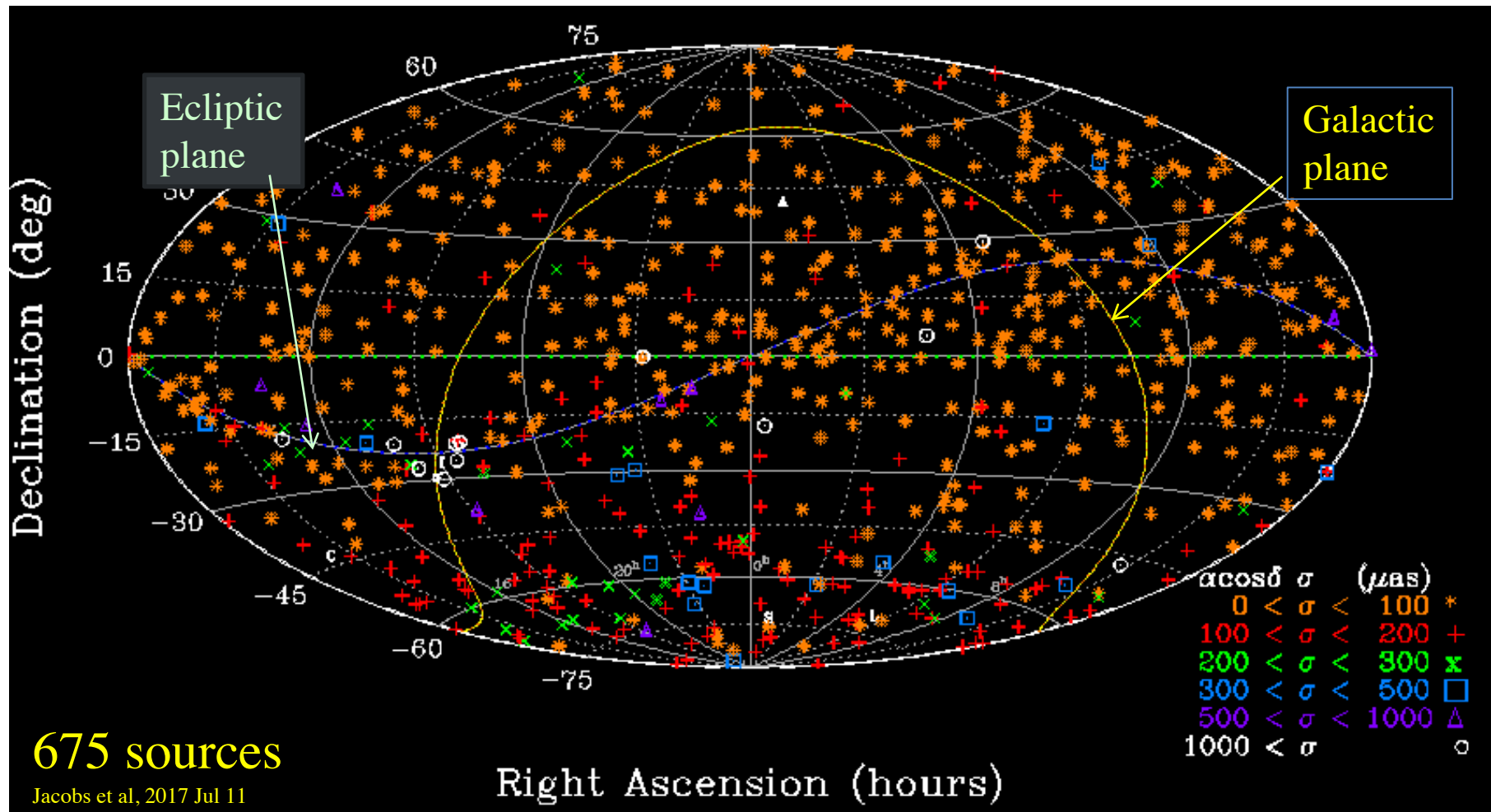
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  - South ( $\delta < -30$  deg) weak due to limited HartRAO, South Africa to Hobart, Tasmania data

# Imaging: VLBA at 24 GHz (1.2cm) (de Witt et al, 2016)



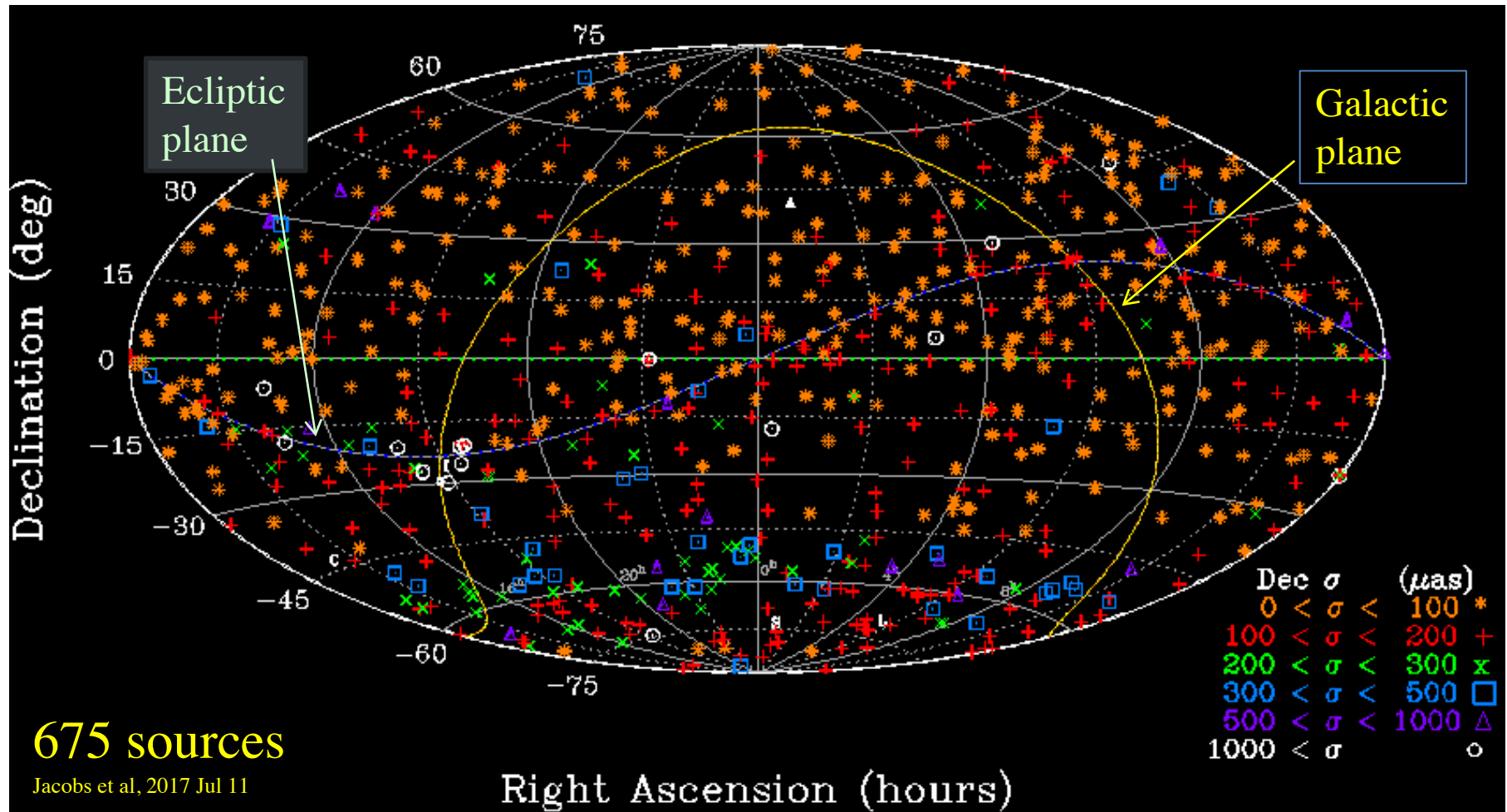
K-band (24 GHz) imaging shows VLBI sources are compact on millarcsec scales.  
Data for 500+ sources acquired. Processing limited by available analyst resources.  
Imaging will be prioritized as comparison outliers pinpoint sources of interest



- **Strengths:**
  - Uniform spatial density
  - less structure than S/X (3.6cm)
  - precision  $< 100 \mu\text{as}$
  - needed only 60K observations vs. SX's 12 million!

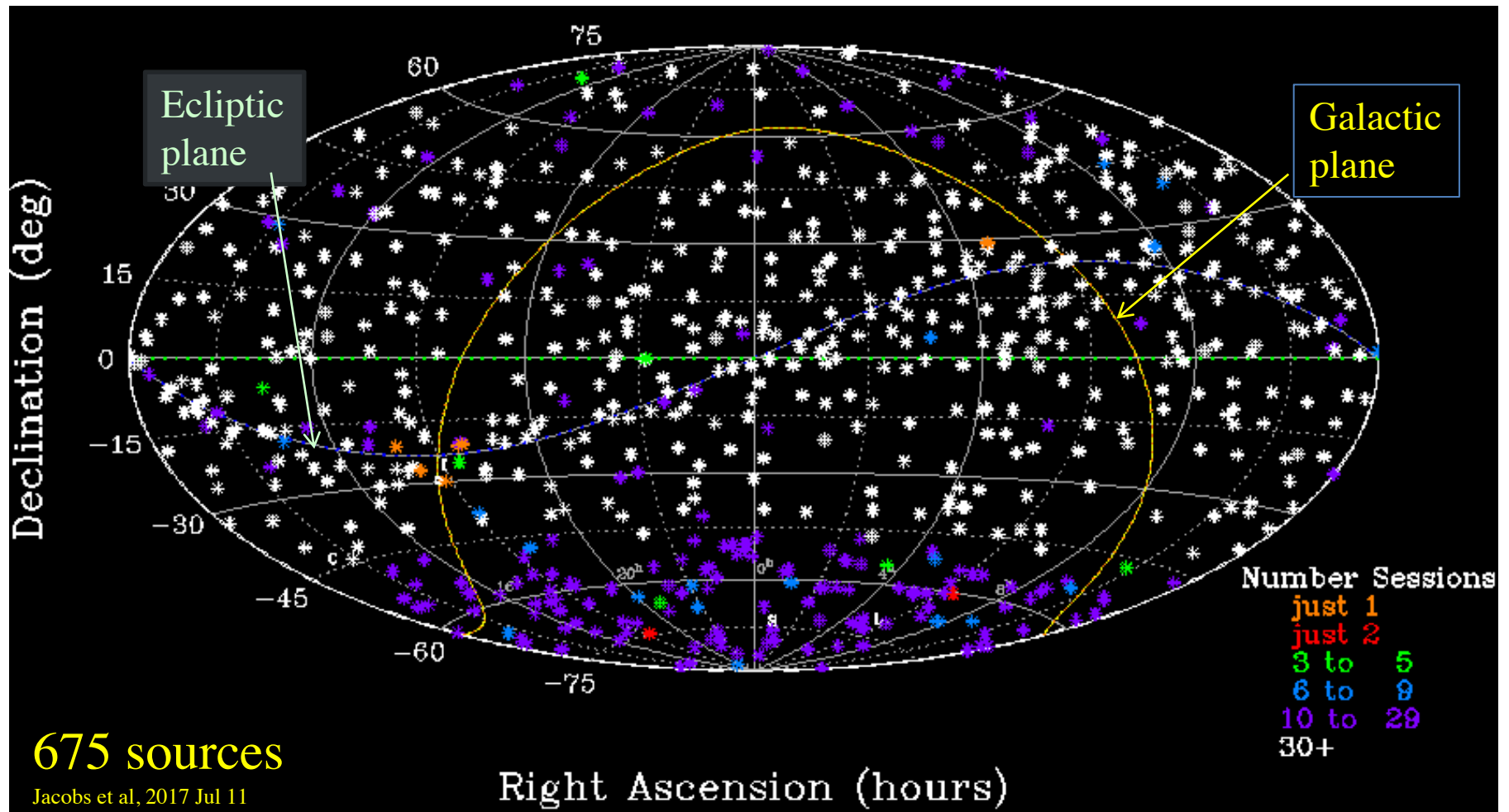
- **Weaknesses:**
  - Poor near Galactic center due to inter-stellar media scattering
  - South weak due to limited time on ESA's Argentina station
  - Limited Argentina-California data makes vulnerable to  $\delta$  zonals
  - Limited Argentina-Australia weakens  $\delta$  from -45 to -60 deg





- **Strengths:**
  - Uniform spatial density
  - less structure than S/X (3.6cm)
  - precision < 100  $\mu$ as
  - needed only 60K observations vs. SX's 12 million!

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  - precision < 100  $\mu$ as
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  - Limited Argentina-California data makes vulnerable to  $\delta$  zonals
  - Limited Argentina-Australia weakens  $\delta$  from -45 to -60 deg



# Ka-band combined NASA/ESA Deep Space Net



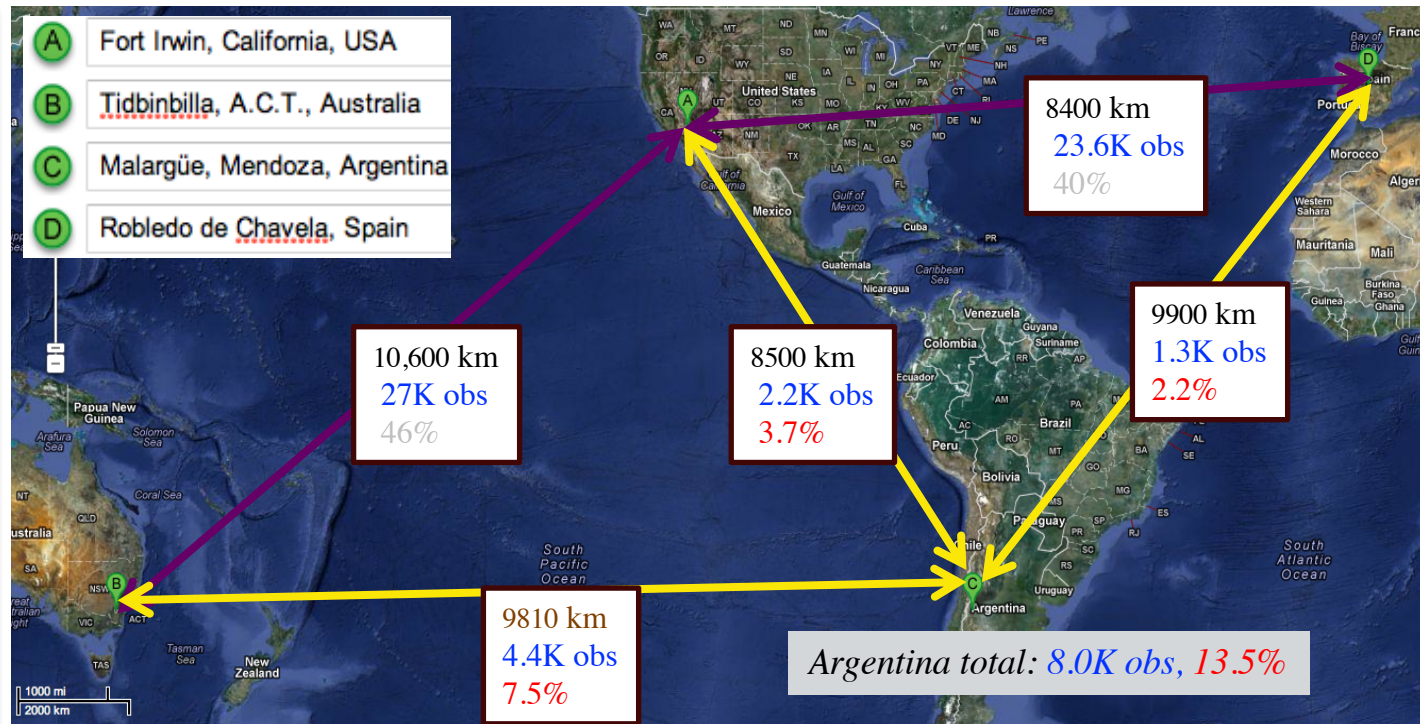
ESA Argentina to NASA-California under-observed by order of magnitude!

## Baseline percentages

- Argentina is part of 3/5 baselines or 60%  
but only 13% of obs
- Aust- Argentina 7.5%
- Spain-Argentina 2.2%
- Calif- Argentina 3.7%

This baseline is under-observed by a factor of ~ 12.

More time on ESA's Argentina station would have a huge, immediate impact!!



Maps credit: Google maps

ESA's Argentina 35-meter antenna **adds 3 baselines** to DSN's 2 baselines

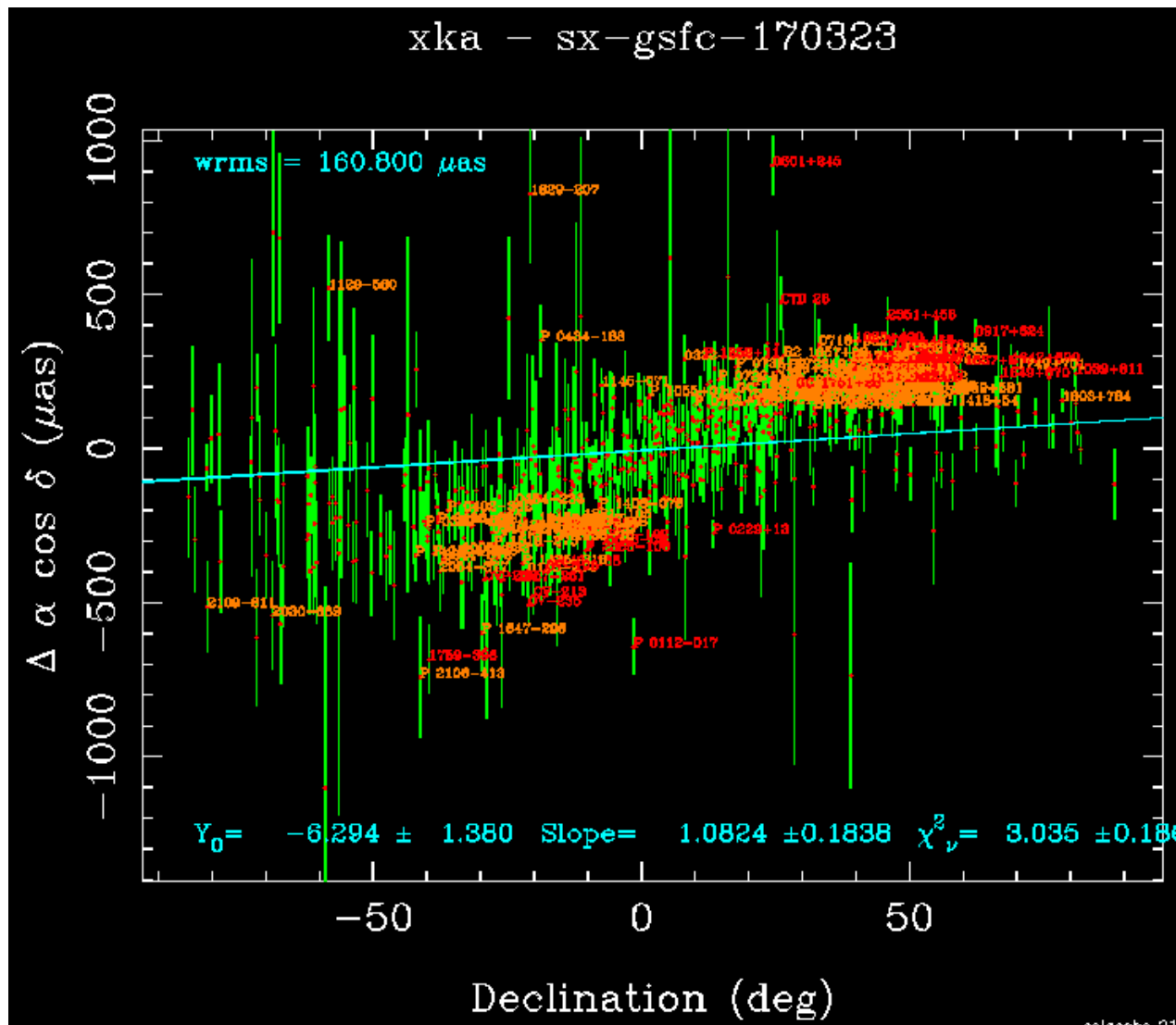
- Full sky coverage by accessing south polar cap
- near perpendicular mid-latitude baselines: CA to Aust./Argentina

### Zonal Errors

- $\Delta\text{RA}$  vs. Dec:  
 $\sim 300 \mu\text{as}$  in south,  $200 \mu\text{as}$  in north
- Need 2 baselines to get 2 angles:  
California-Canberra: 24K obs  
California-Argentina: 2K obs
- > Need more California-Argentina data to overcome this 12 to 1 distortion in sampling geometry.  
ESA's Malargüe is key.
- Usuda, Japan 54-m XKa (2019) would improve North-South sampling geometry and thus control declination zonal differences.



### XKa vs. SX: Zonal errors



The goal:

Alignment of Optical and Radio  
into Common Frame



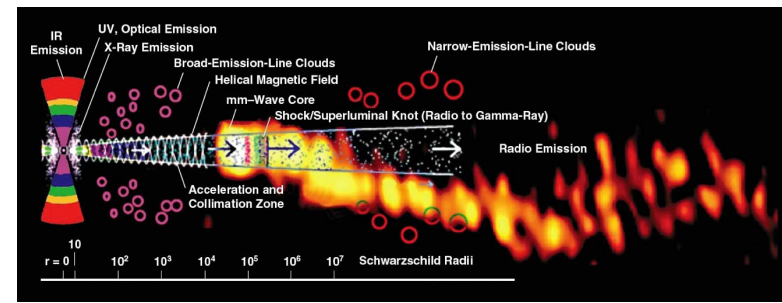
# Optical-Radio Frame Tie Geometry

Determine 3 small rotations ( $R_{1,2,3}$ ) and zonal differences i.e. spherical harmonics  $Y_{lm}$  between the individually rigid, non-rotating **radio** and **optical** frames to sub-part per billion level

Allows seamless integration into united frame.

**More than 1 billion objects will be integrated into common frame!!**

**Object precision to  $< 100 \mu\text{as}$ , 0.5 ppb. want tie errors 10 times smaller.**

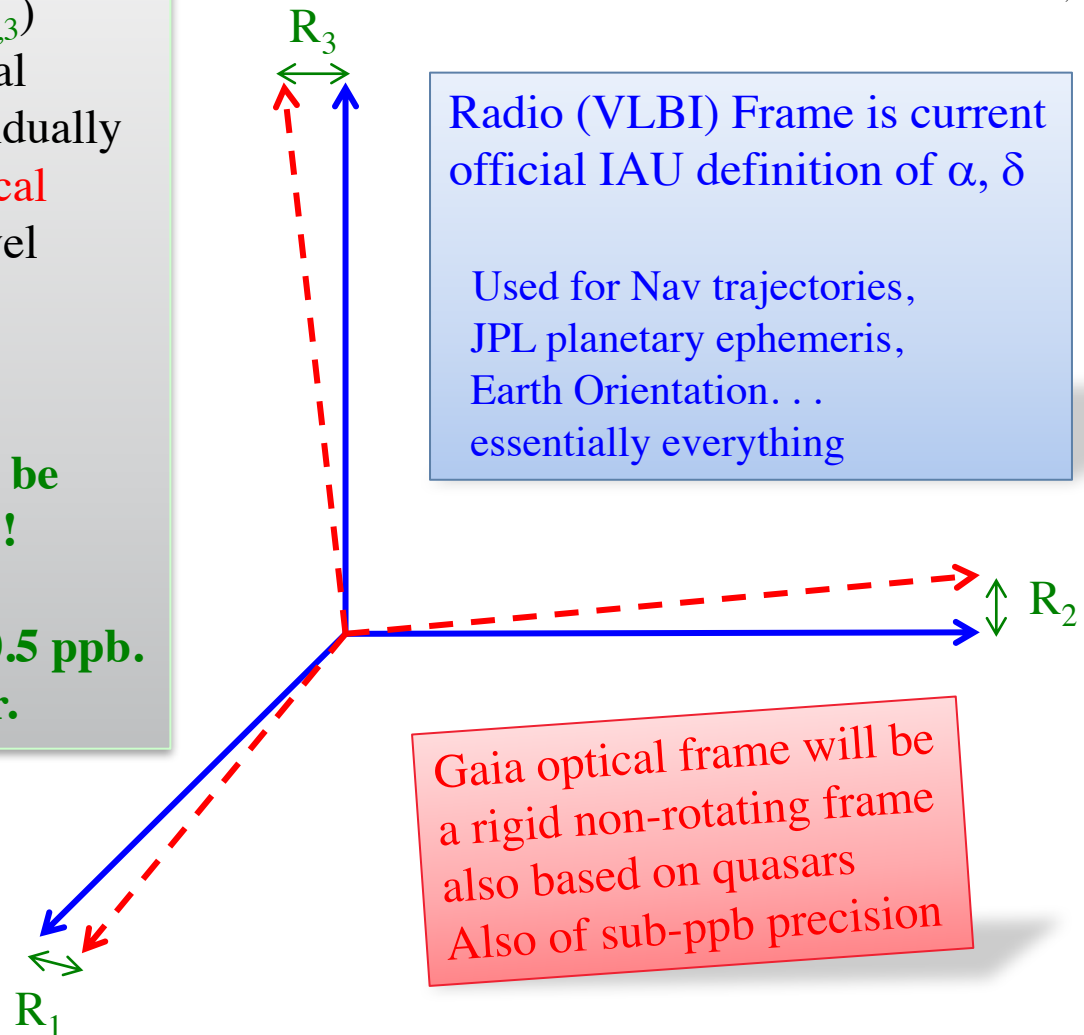


Credit: Marscher+, Krichbaum+

Radio (VLBI) Frame is current official IAU definition of  $\alpha, \delta$

Used for Nav trajectories,  
JPL planetary ephemeris,  
Earth Orientation. . .  
essentially everything

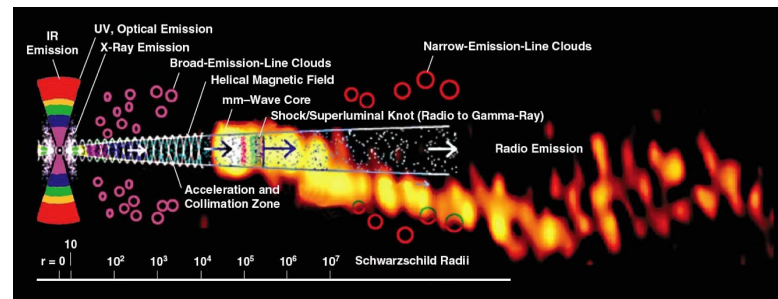
Gaia optical frame will be  
a rigid non-rotating frame  
also based on quasars  
Also of sub-ppb precision



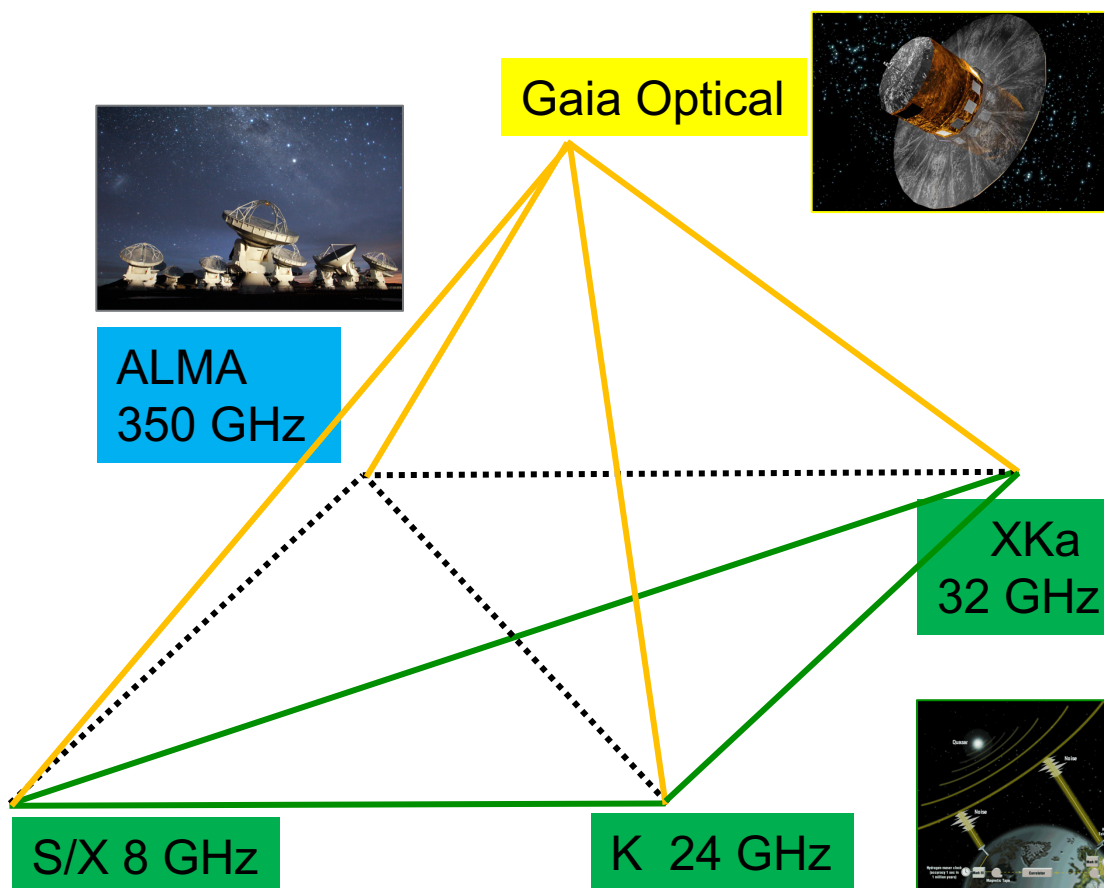
# Frame Tie Comparisons

## Tying Optical and Radio Celestial Frames

Systematics to be flushed out via  
Inter-comparison of multiple high  
precision frames.



Credit: Marscher+, Krichbaum+



### Systematics:

Gaia: 60 mas beam sees  
Host galaxy, foreground stars, etc.

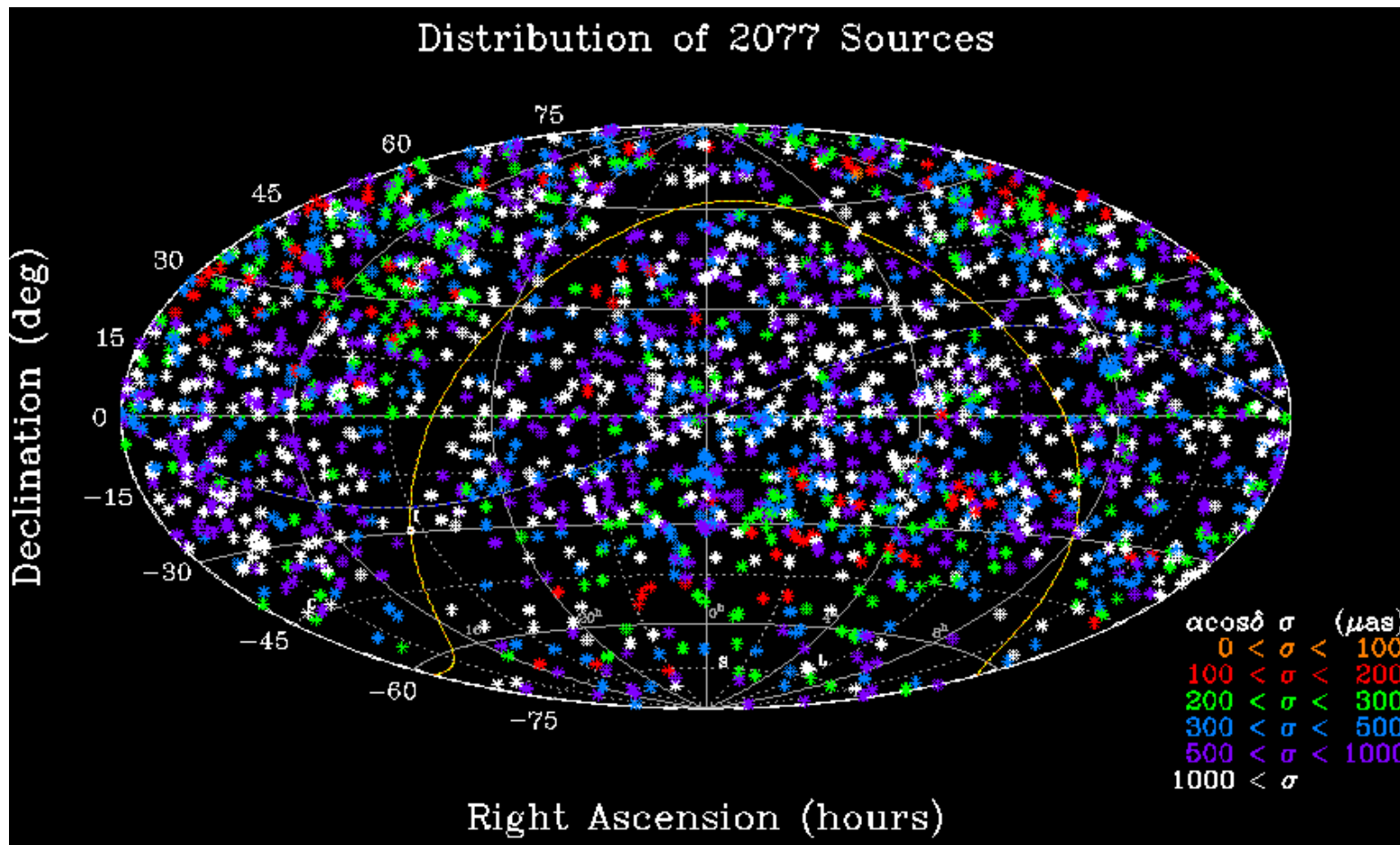
ALMA: pilot obs bright end  $\sim 5^{\text{mag}}$   
Waiting on 10km+ configurations

VLBI: All bands need more  
southern data

S/X: Source structure  
K: Ionosphere  
XKa: Argentina baselines  
under-observed

# Tying optical and Radio Celestial Frames

## Gaia DR1-aux vs. SX VLBI



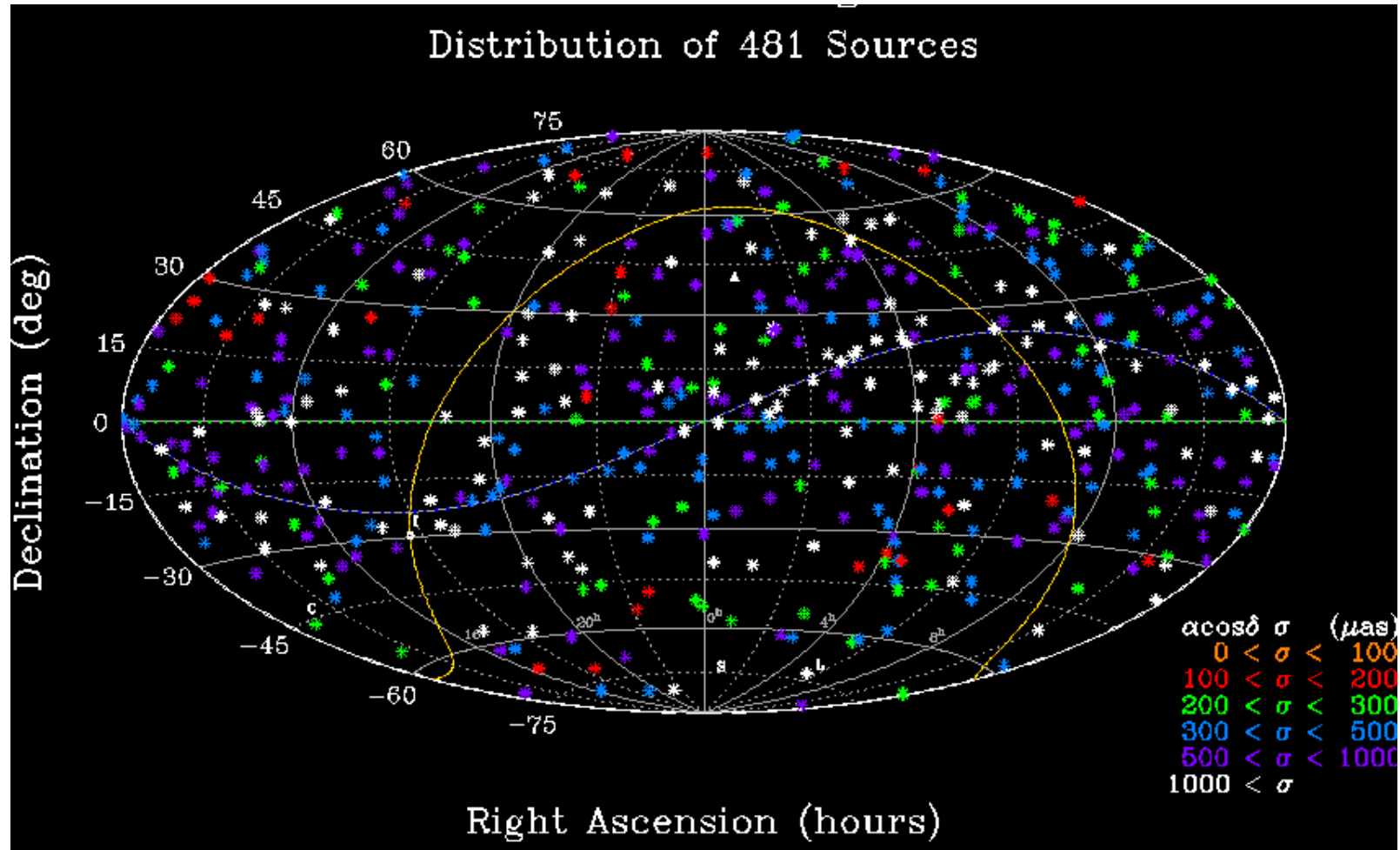
~5 times more sources than K or Ka

Fairly uniform distribution. A bit weaker in the south

Color code shows Gaia formal sigmas.

# Tying optical and Radio Celestial Frames

## Gaia DR1-aux vs. K VLBI



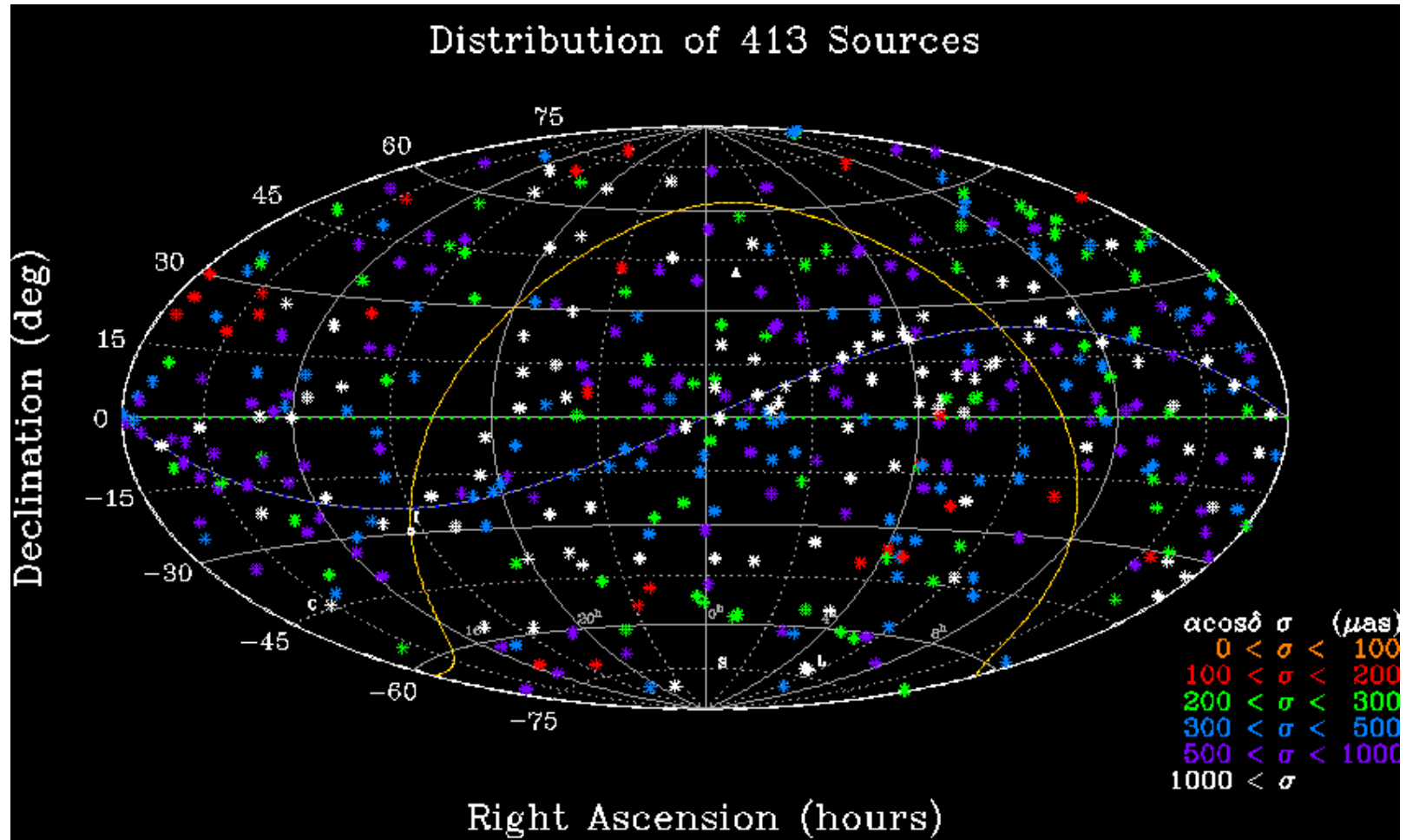
Fairly uniform distribution.

Color code shows Gaia formal sigmas.

# Tying optical and Radio Celestial Frames



## Gaia DR1-aux vs. Ka VLBI



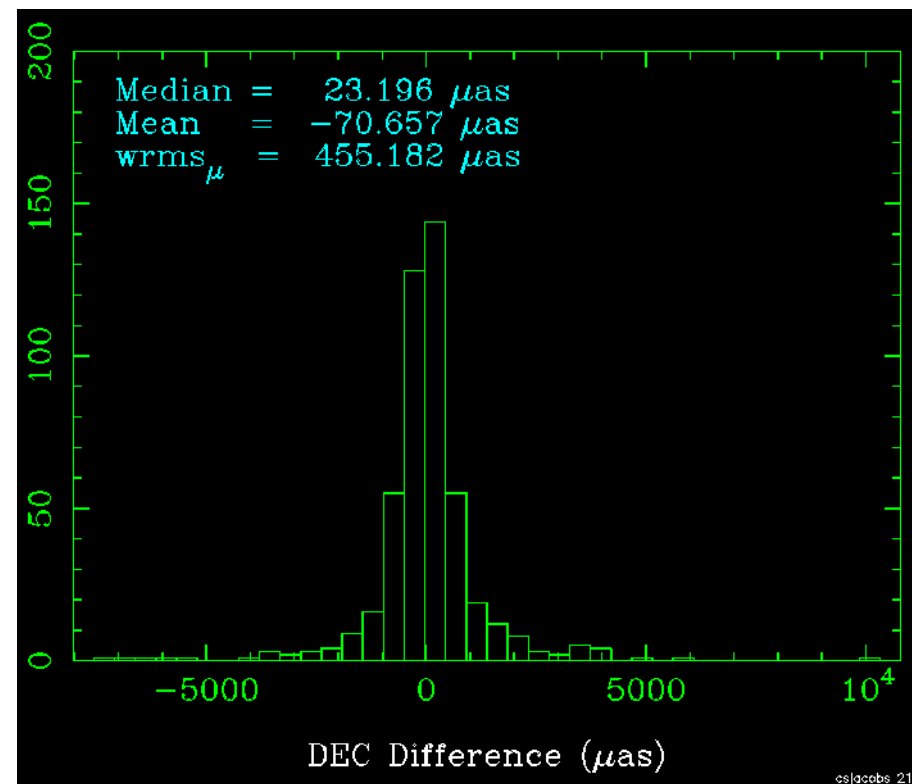
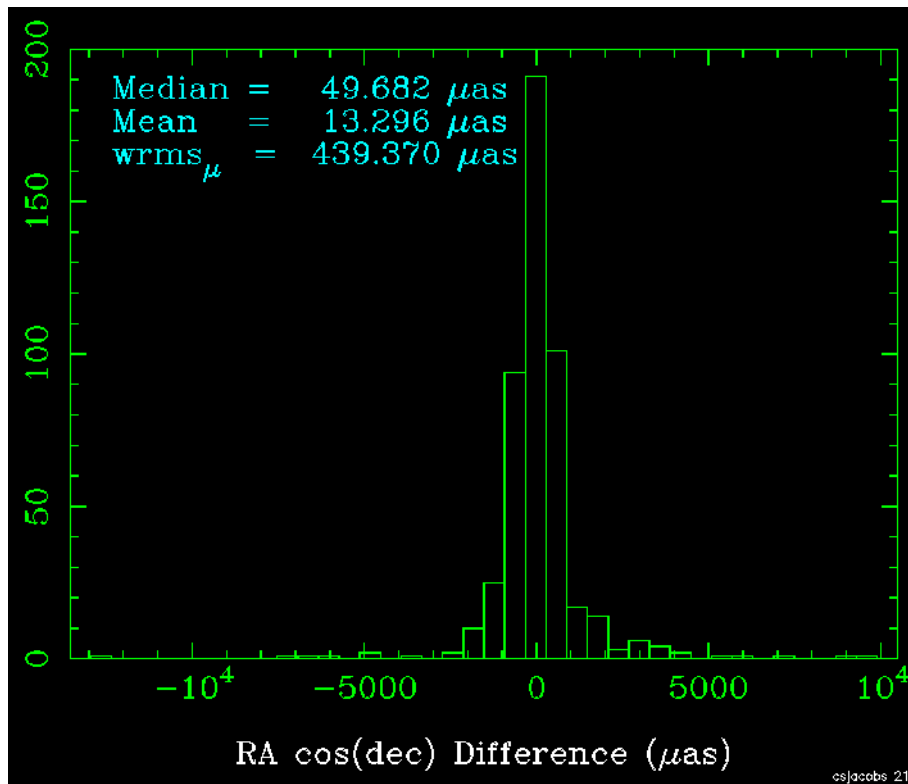
Fairly uniform distribution.

Color code shows Gaia formal sigmas.





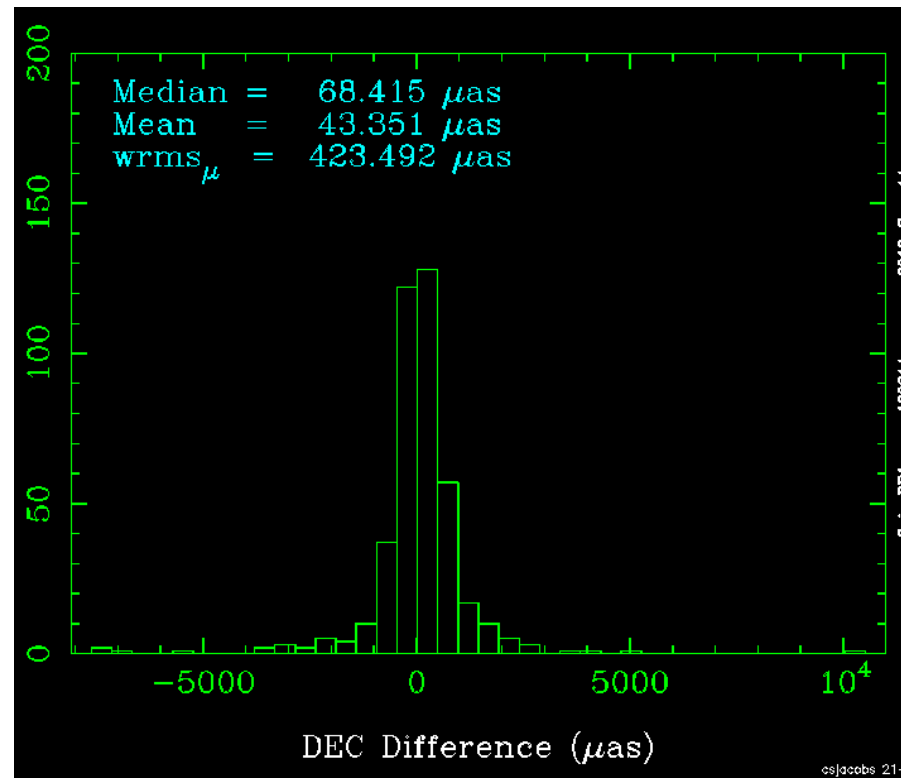
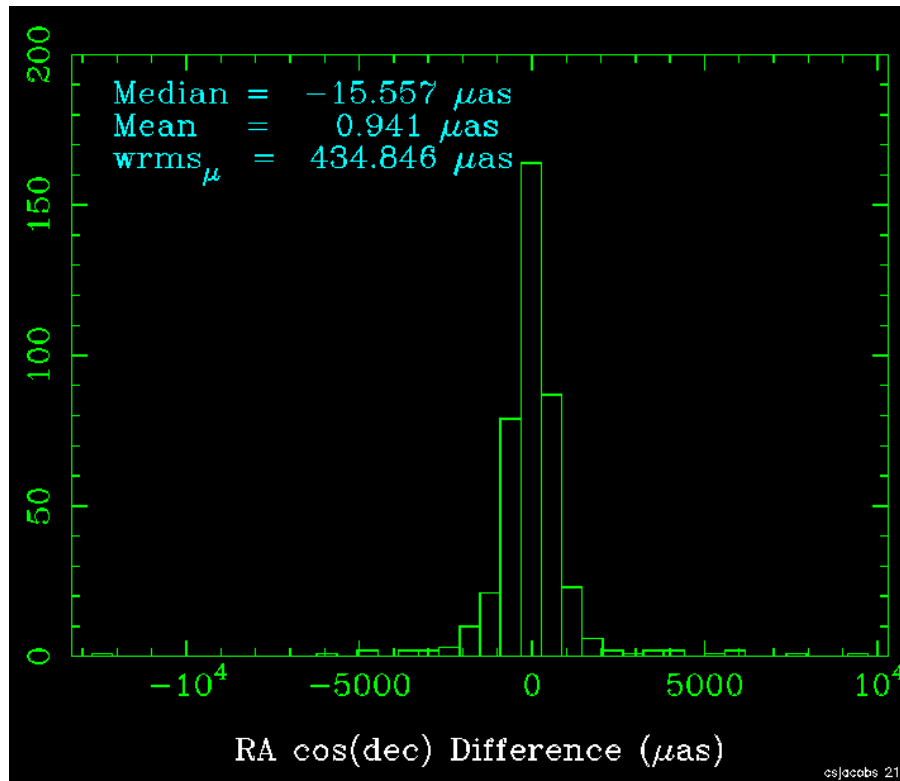
## Gaia DR1-aux vs. K VLBI



wRMS Ra and Dec differences about 440  $\mu\text{as}$  (2 nrad)  
Normalized differences are about 1.1 indicating realistic errors



## Gaia DR1-aux vs. Ka VLBI

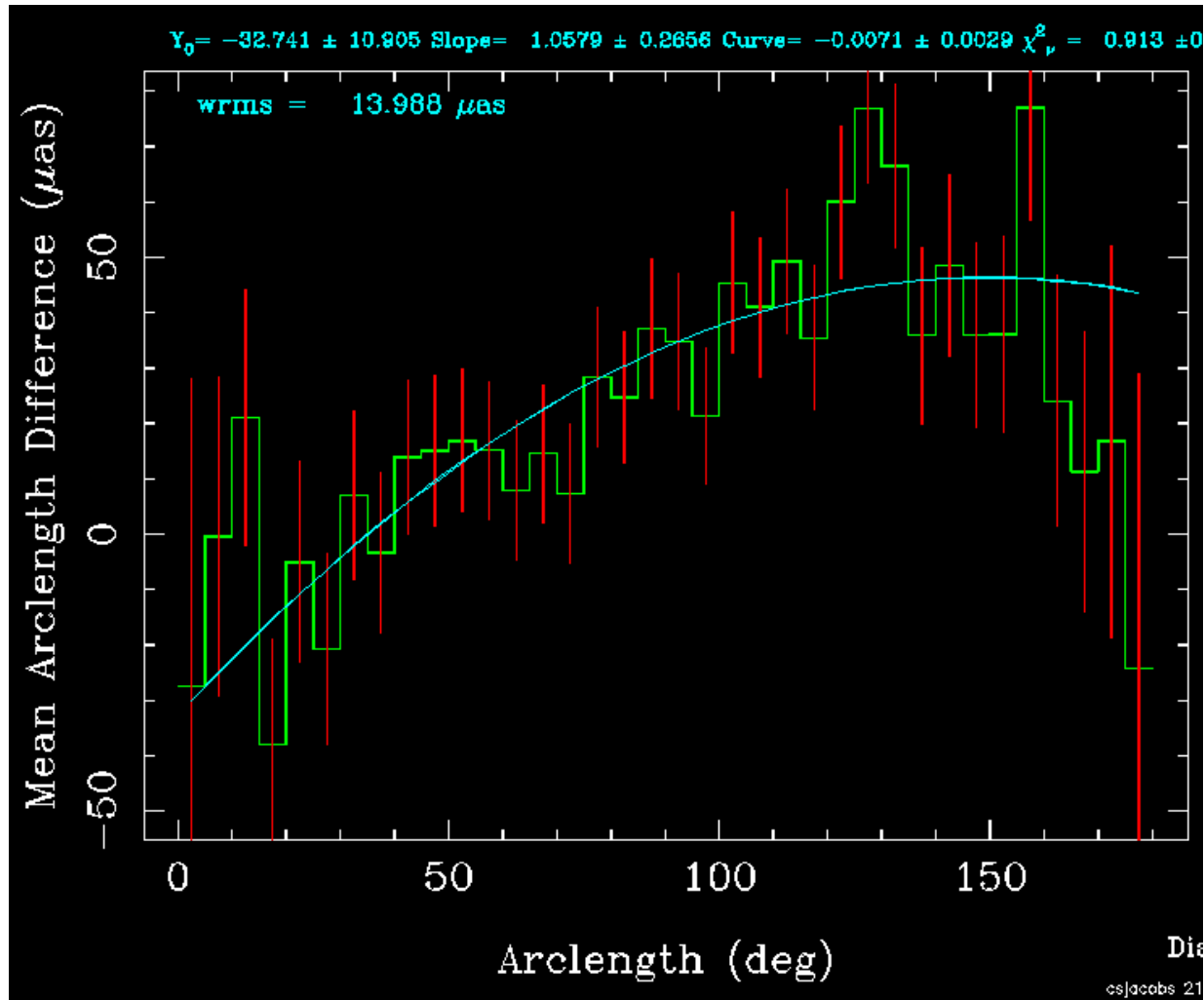


wRMS Ra and Dec differences about  $400 \mu\text{as}$  (2 nrad)  
Normalized differences are about 1.1 indicating realistic errors

# Tying optical and Radio Celestial Frames



## Gaia DR1-aux vs. K VLBI

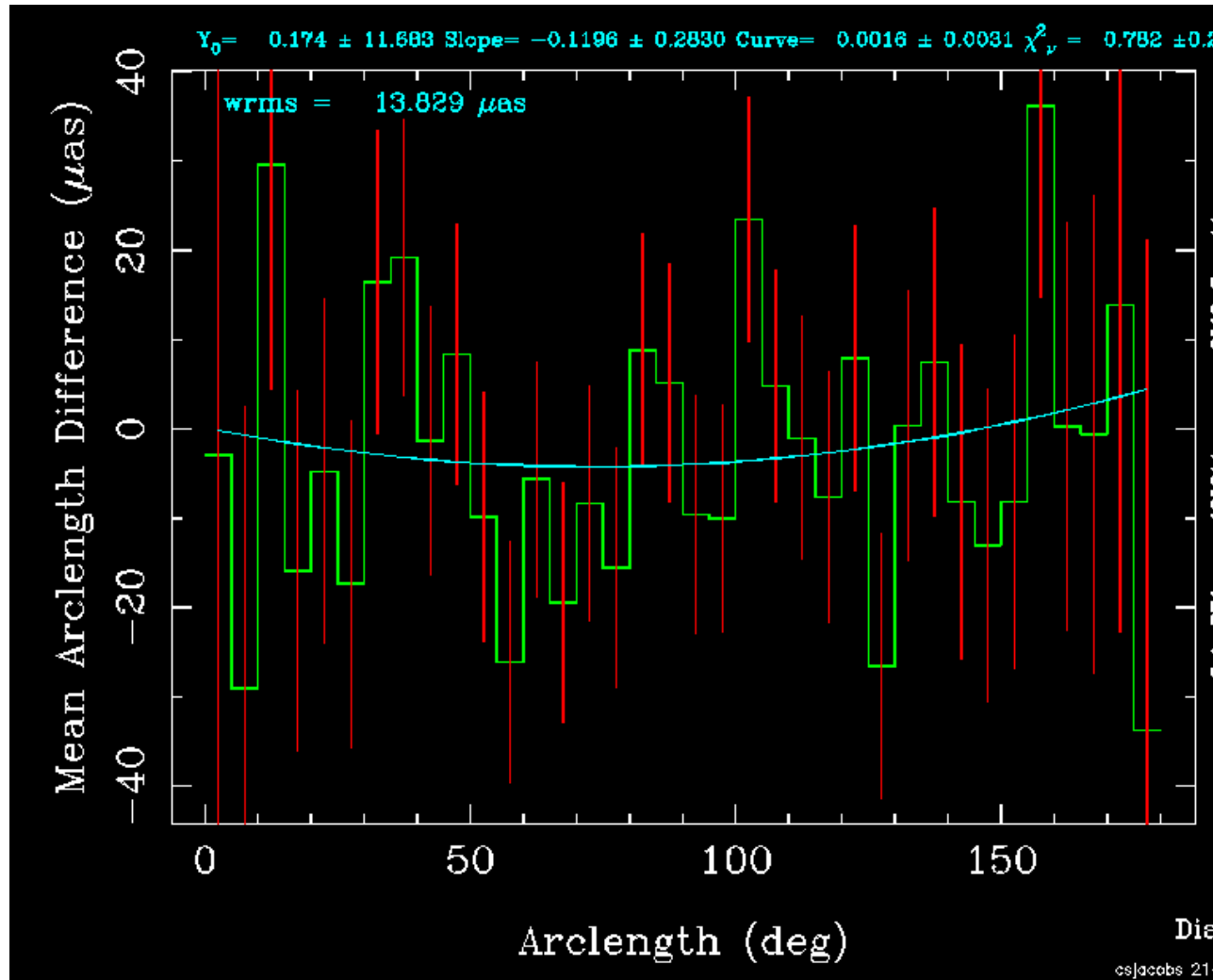


Arc differences vs. arclength bins show distortion at  $50 \mu\text{as}$  level

# Tying optical and Radio Celestial Frames



## Gaia DR1-aux vs. Ka VLBI



Arc differences steady vs. arc length bins at  $15 \mu\text{as}$  level



# Gaia DR1-aux vs. SX VLBI

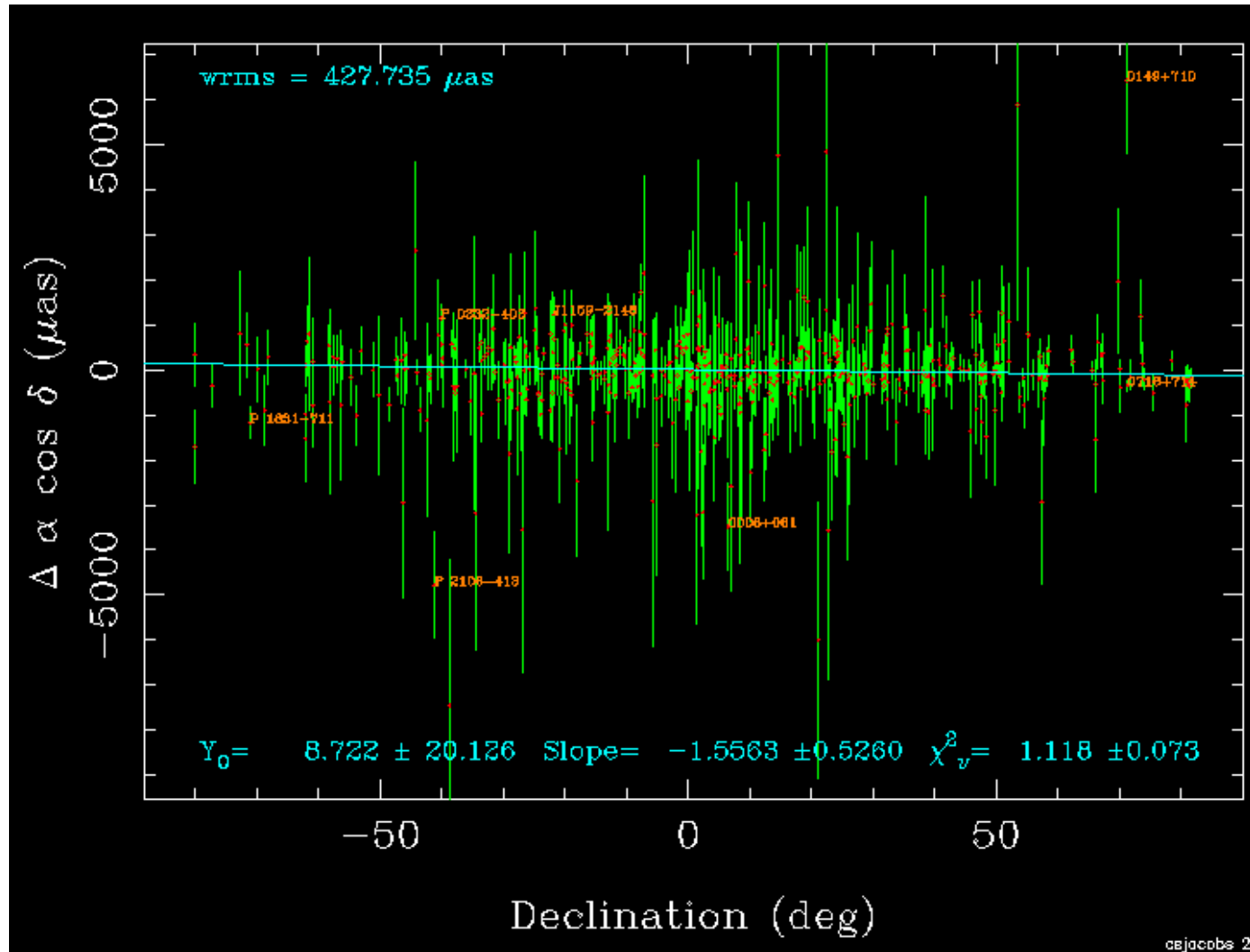


Systematic tilt:  $\Delta\alpha$  vs.  $\delta$  has 2 sigma slope of  $-0.46 \pm 0.25 \mu\text{as/deg}$

# Tying optical and Radio Celestial Frames



## Gaia DR1-aux vs. K VLBI

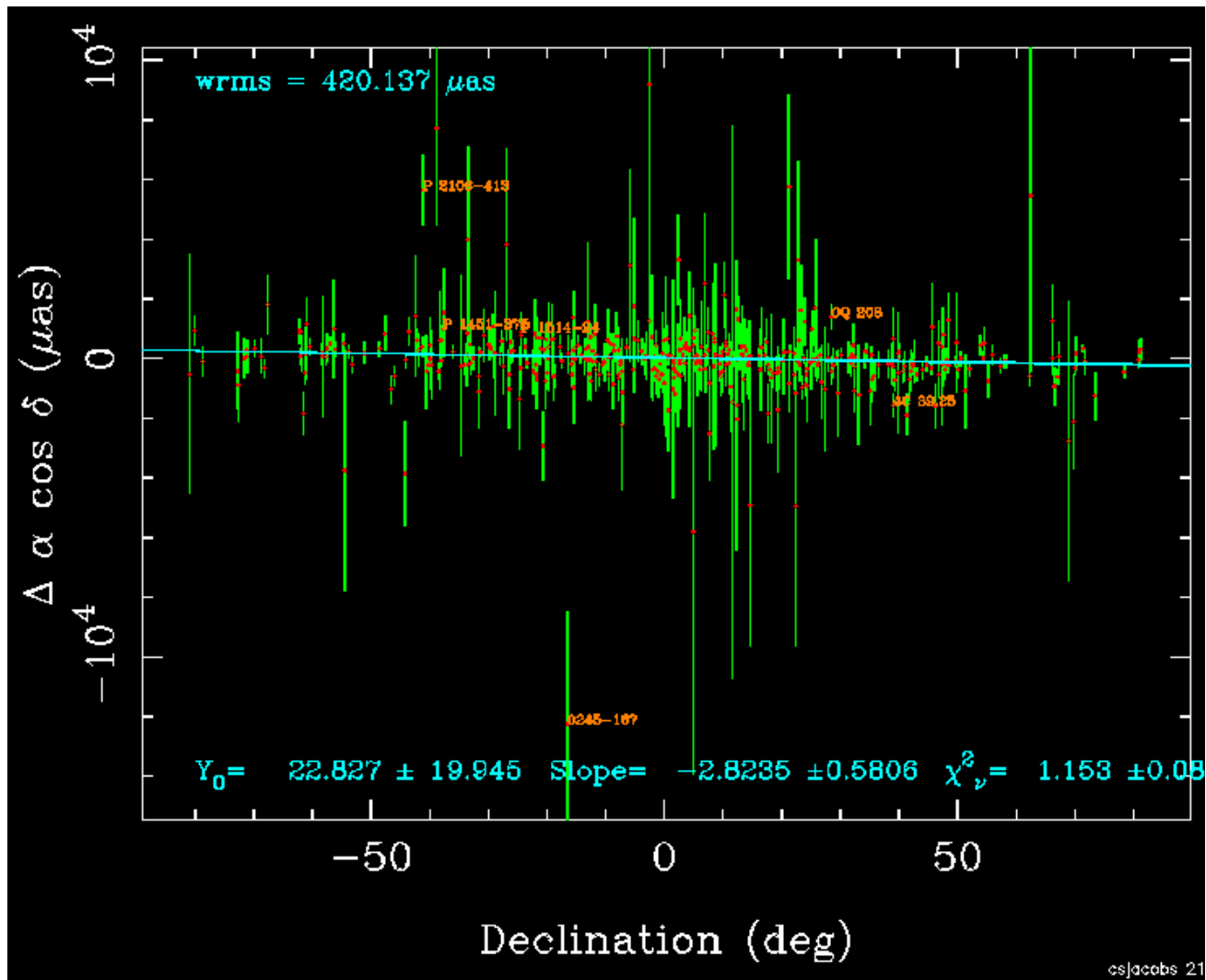


Systematic tilt:  $\Delta \alpha$  vs.  $\delta$  has 3 sigma slope of  $-1.56 \pm 0.53 \mu\text{as/deg}$

# Tying optical and Radio Celestial Frames



## Gaia DR1-aux vs. Ka VLBI



Systematic tilt:  $\Delta \alpha$  vs.  $\delta$  has 4.9 sigma slope of  $-2.8 \pm 0.6 \mu\text{as/deg}$

# Tying optical and Radio Celestial Frames

## Gaia DR1-aux vs. VLBI



	SX-band 8 GHz 3.6cm	K-band 24 GHz 1.2 cm	XKa-band 32 GHz 0.9 cm
# Observations	12 million	0.25 million	0.06 million
# sources	1926	473	405
# outliers $> 5\sigma$	100	13	6
% outliers	5.2 %	2.7 %	1.5 %
$\alpha$ wRMS	523 $\mu$ as	431 $\mu$ as	433 $\mu$ as
$\delta$ wRMS	531 $\mu$ as	453 $\mu$ as	418 $\mu$ as
$R_x$	-37 $\pm$ 13	-89 $\pm$ 24	57 $\pm$ 24
$R_y$	0 $\pm$ 11	14 $\pm$ 21	32 $\pm$ 21
$R_z$	-29 $\pm$ 13	-13 $\pm$ 23	21 $\pm$ 24
$\Delta\alpha$ vs. $\delta$ tilt ( $\mu$ as/deg)	-0.46 $\pm$ 0.25	-1.55 $\pm$ 0.53	-2.83 $\pm$ 0.58

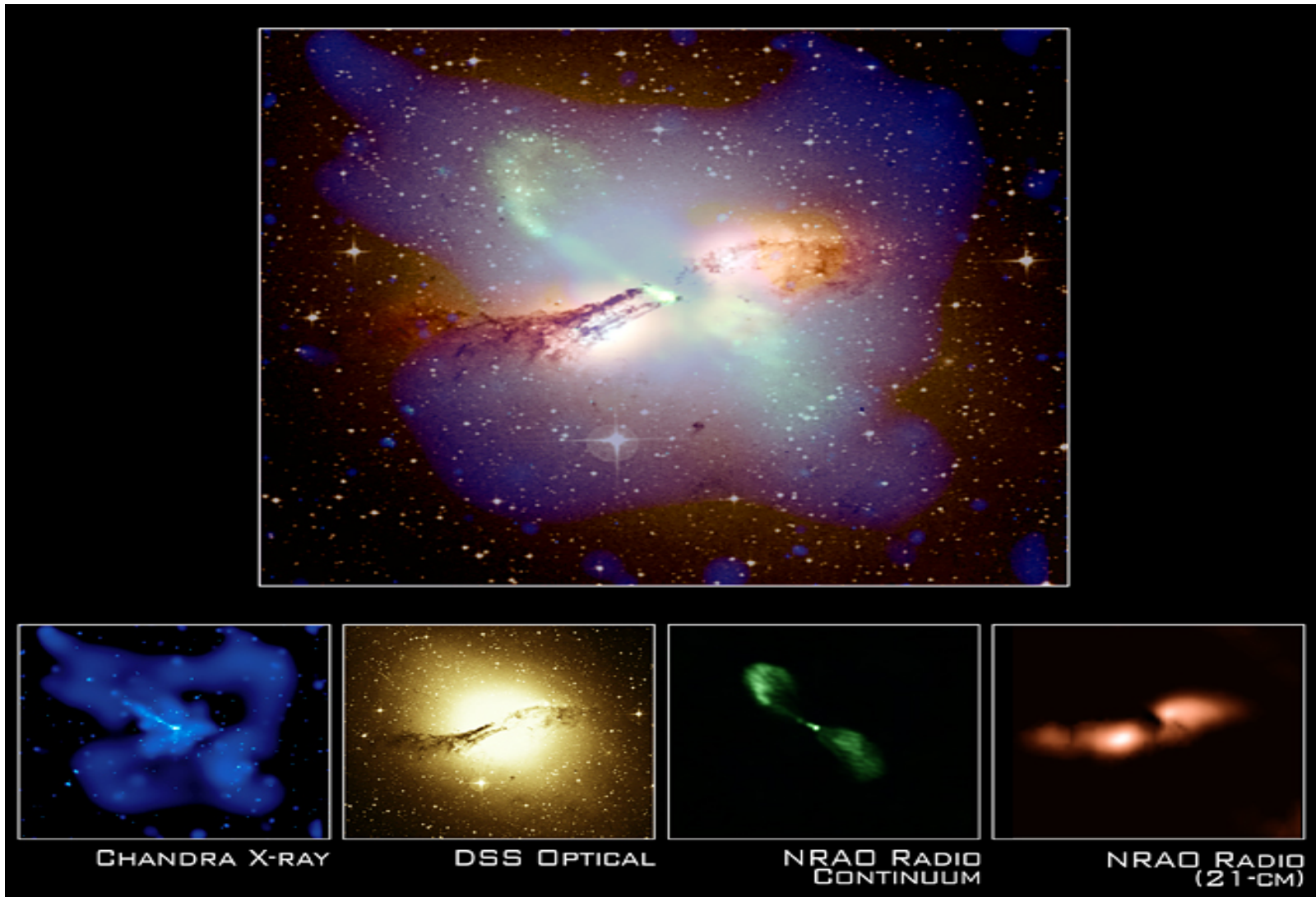
Rx vulnerable  
To trop errors

Hints that results improve by going to higher radio frequency  
However, the above results do not use exact same objects



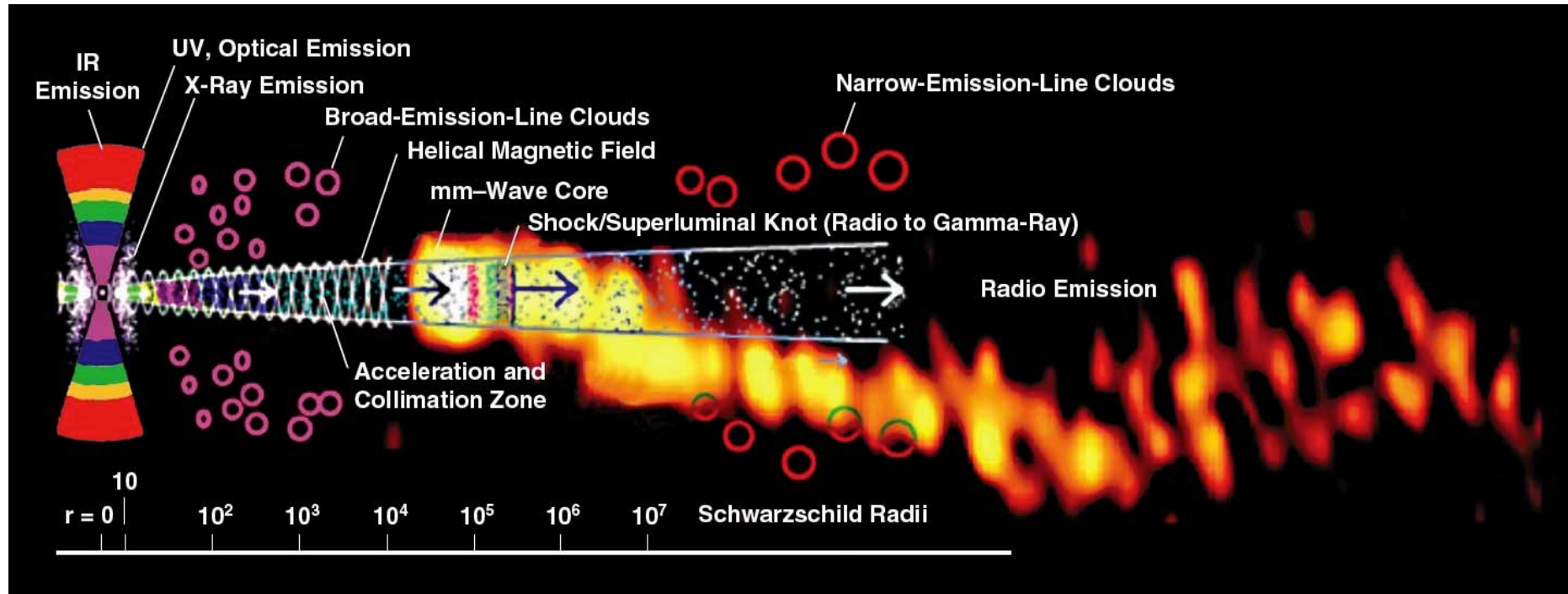
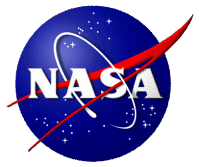
# A last look at Optical vs. Radio Astrometric offsets

# Example Extragalactic Source: Centaurus-A in X-ray, Optical, Radio



Credits: X-ray (NASA/CXC/M. Karovska et al.); Radio 21-cm image (NRAO/VLA/Schiminovich, et al.),  
Radio continuum image (NRAO/VLA/J. Condon et al.); Optical (Digitized Sky Survey U.K. Schmidt Image/STScI)

# Active Galactic Nuclei (*Marscher*)



$R \sim 0.1 - 1 \mu\text{as}$

$1 \text{ mas}$

Features of AGN: *Note the Logarithmic length scale.*

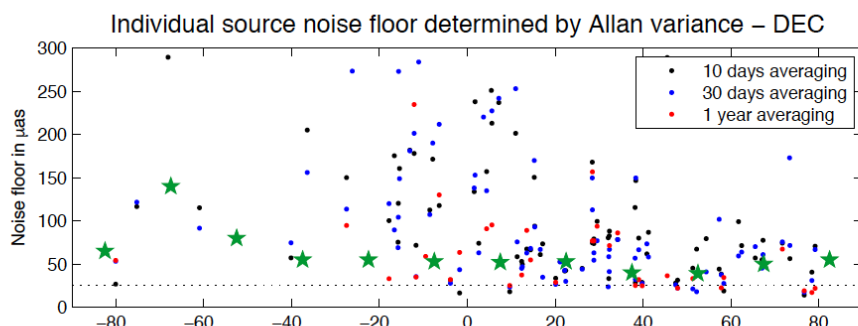
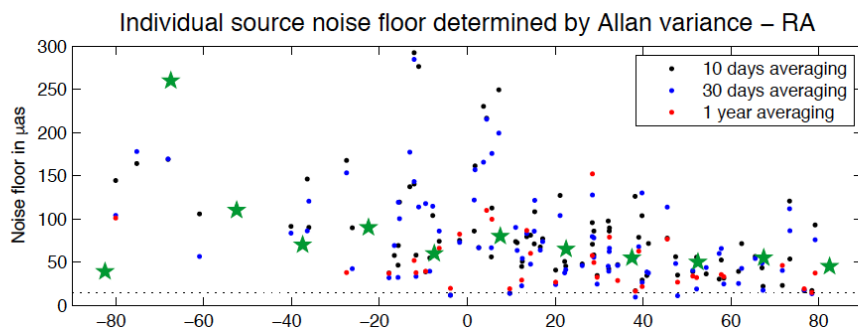
“Shock waves are frequency stratified, with highest synchrotron frequencies emitted only close to the shock front where electrons are energized. The part of the jet interior to the mm-wave core is opaque at cm wavelengths. At this point, it is not clear whether substantial emission occurs between the base of the jet and the mm-wave core.”

*Credits: Alan Marscher, 'Relativistic Jets in Active Galactic Nuclei and their relationship to the Central Engine,' Proc. of Science, VI Microquasar Workshop: Microquasars & Beyond, Societa del Casino, Como, Italy, 18-22 Sep 2006. Overlay (not to scale): 3 mm radio image of the blazar 3C454.3 (Krichbaum et al. 1999)*

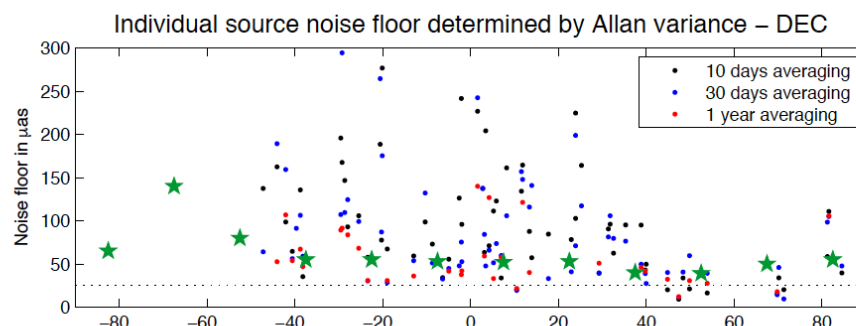
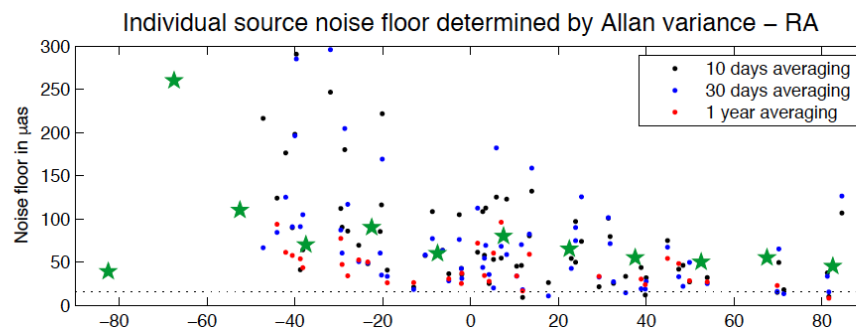
# SX VLBI systematic Floor $\sim 20$ to $30 \mu\text{as}$ ?



## Set of Flicker Noise sources



## Set of White Noise sources



Green ★ : ICRF2 noise floor - average on sources in  $15^\circ$  declination bands.

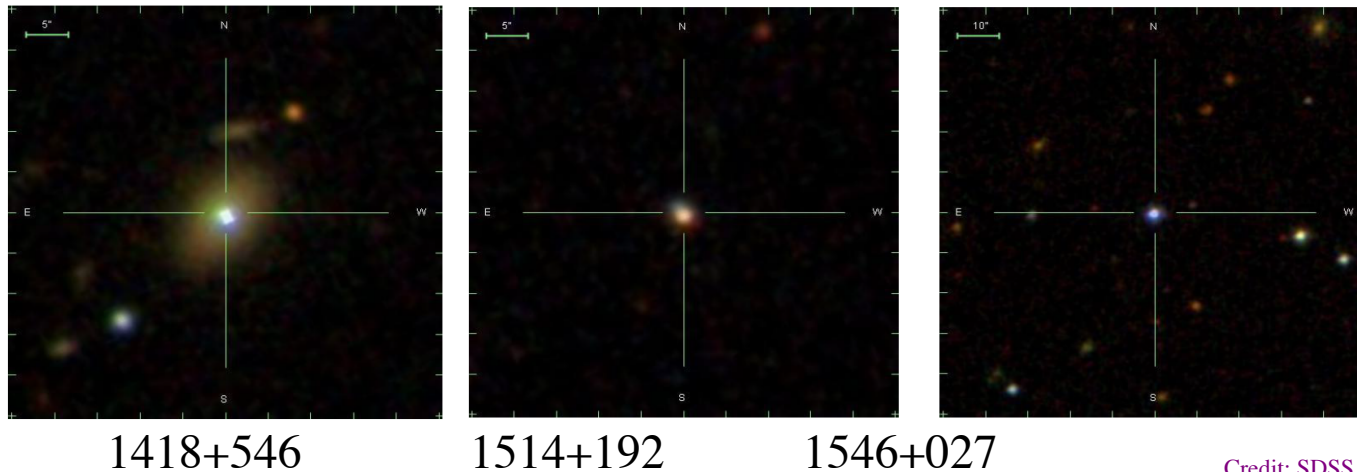
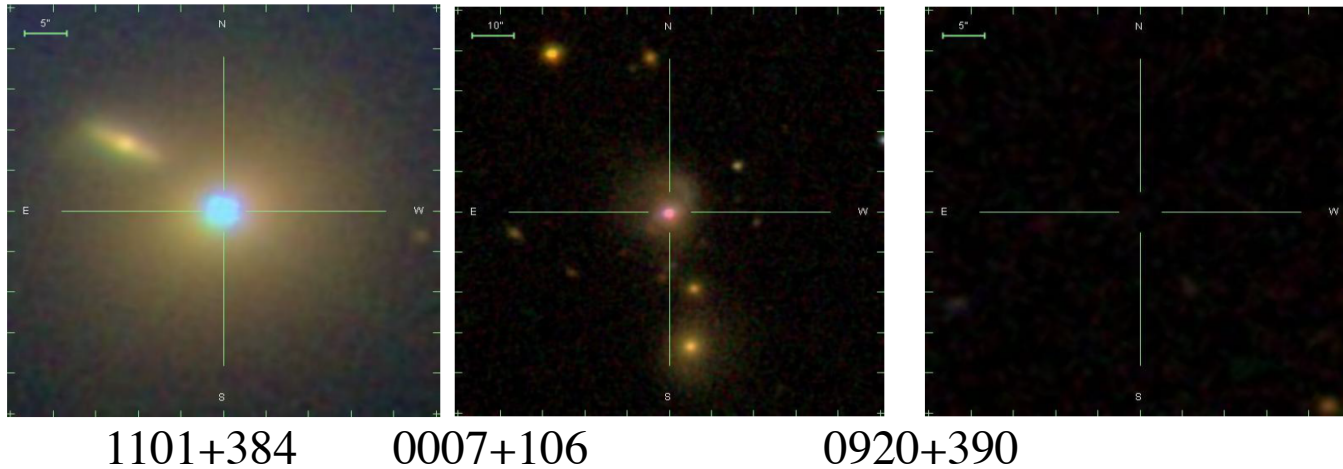
Attention! This method uses ALL “good” sessions, contrary to the decimation test.

Le Bail+ (EVGA, 2017) use Allan variance test on position time histories to determine when **averaging no longer helps—systematic floor is encountered.**

**Structure part of this floor should be several times smaller at K (24 GHz) and Ka (32 GHz)**

# Optical vs. Radio systematics offsets

## SDSS Optical images of quasars (scale 5-10 asec)

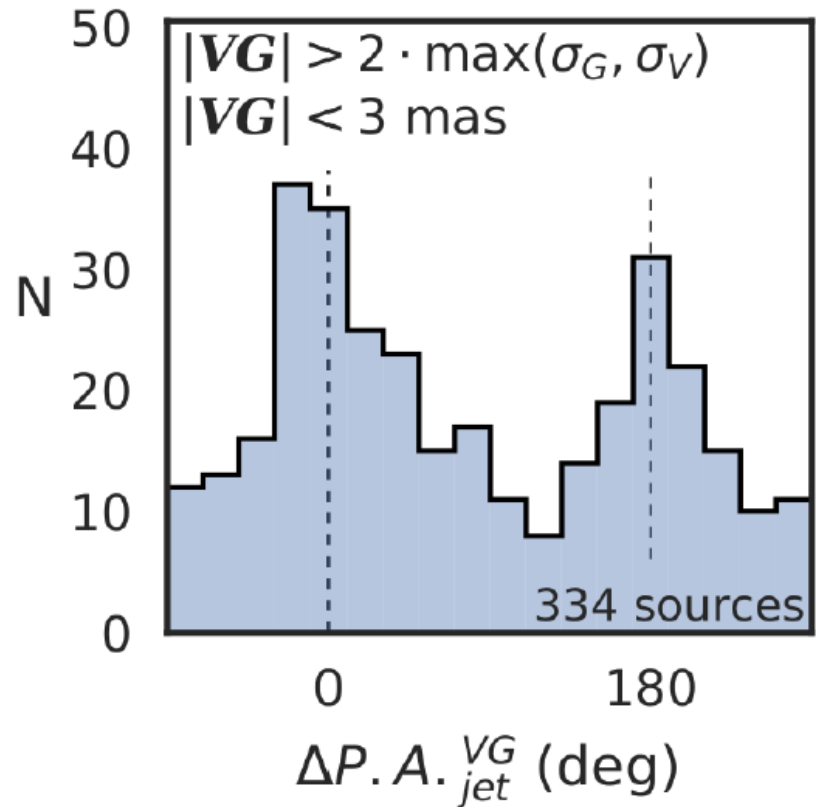
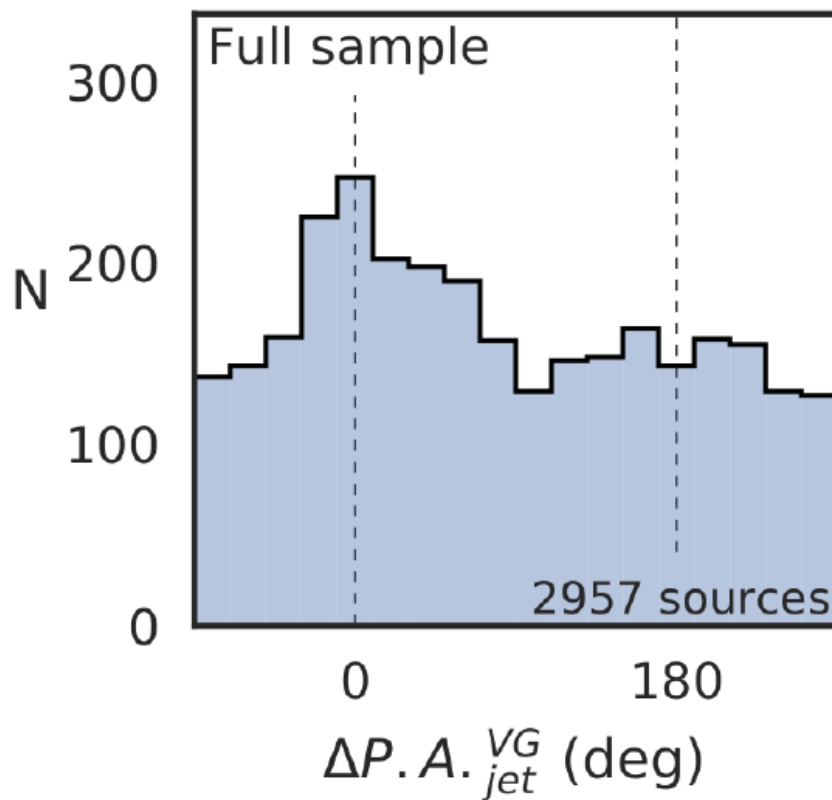
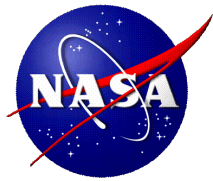


Credit: SDSS

- Optical structure: The host galaxy may not be centered on the AGN or may be asymmetric.
- Optical systematics unknown, fraction of milliarcsecond optical centroid offset?
- Optical imaging generally 10s of milliarcsecond. In general, no sub-mas optical imaging.



# Optical vs. Radio systematics offsets



Petrov & Kovalev (MNRAS, 2017) show that optical-radio astrometric offsets Correlate with jet direction (or anti-direction).

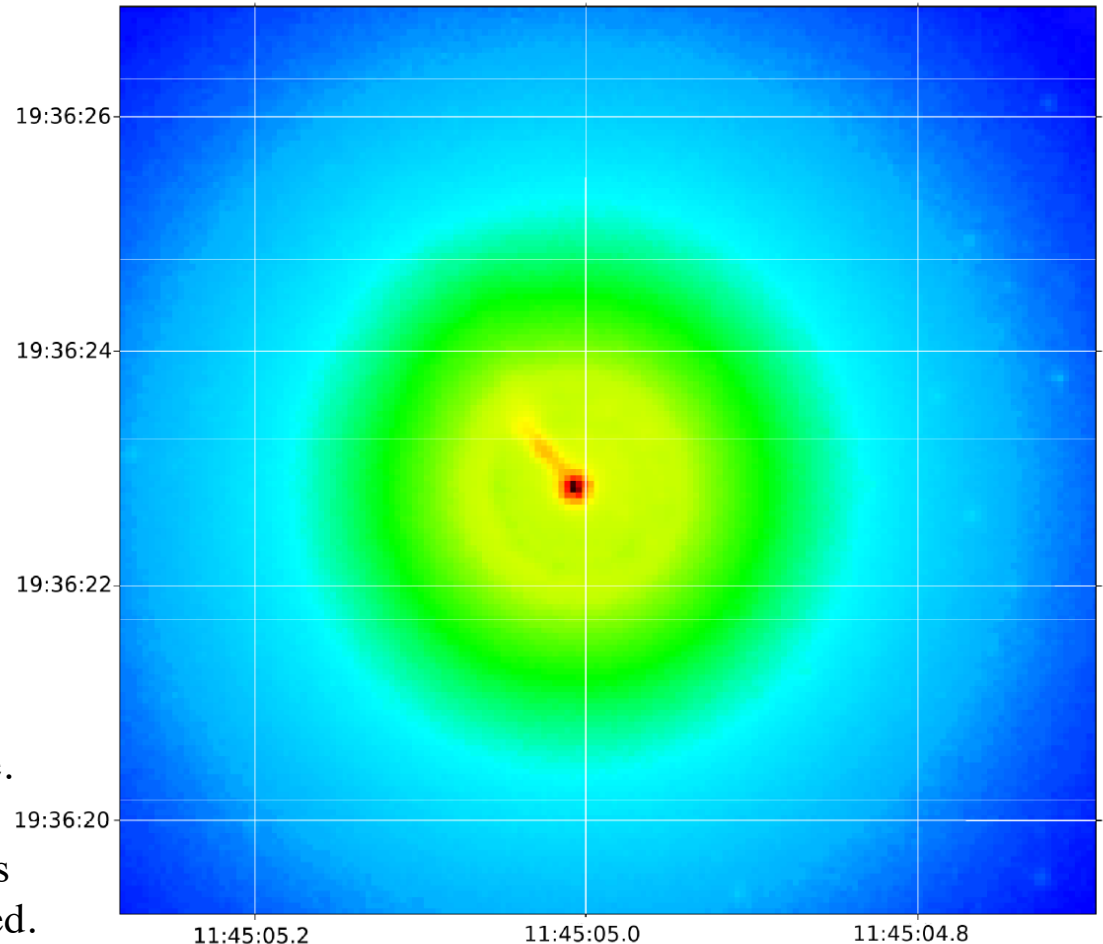
They argue that the offsets are dominated by optical synchrotron jets.

# Optical vs. Radio systematics offsets

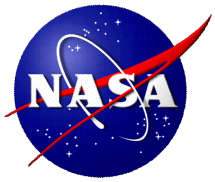


Petrov & Kovalev (MNRAS, 2017)

- Example of optical jet in “nearby” 3C 264 would scale to ~milli-arcsecond offsets at typical AGN distances.
- Optical synchrotron jets may be limiting factor in radio-optical astrometric agreement.
- VLBI interferometry “locks” onto the brightest component. Also extremely high resolution resolves out extended structures. So VLBI positions is close of the core.
- Gaia optical image’s centroid averages all of the light distribution, jet included. “Beam” is 60 milliarcseconds.
- Optical may be more easily biased than radio.



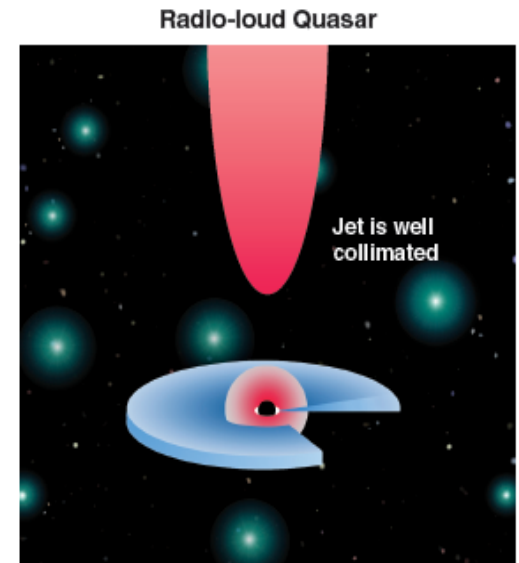
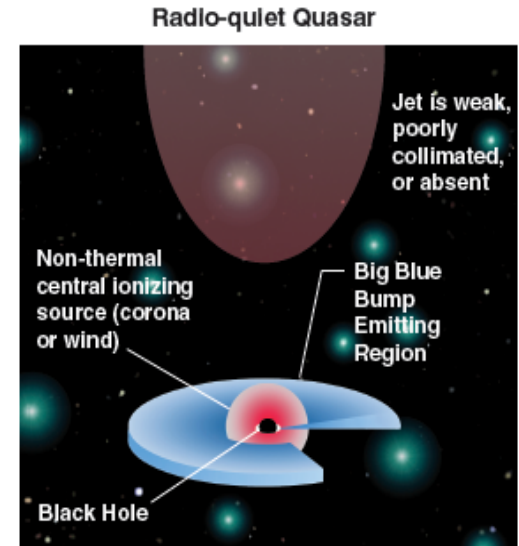
**Figure 3.** The archival HST image of 3C264 at 606 nm, HST project ID 13327 (Meyer et al. 2015).



# Optical vs. Radio positions

Positions differences from:

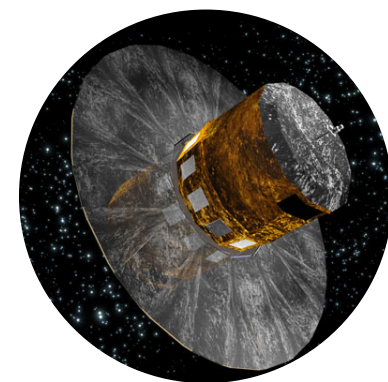
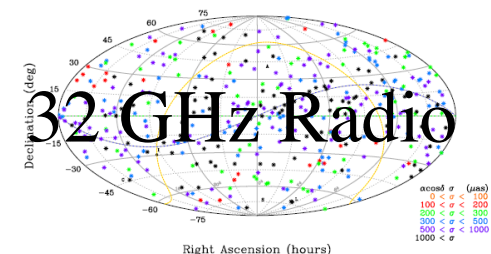
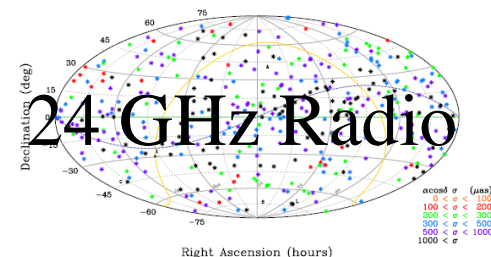
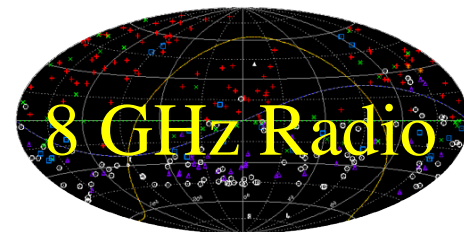
- Astrophysics of emission centroids
  - radio: synchrotron from jet
  - optical: **synchrotron from jet?**  
non-thermal ionization from corona?  
big blue bump from accretion disk?
- Instrumental errors both radio & optical
- Analysis errors





# Summary: Tying Optical & Radio

- **Goal:** Tie of optical and radio celestial frames for deep space navigation and astronomical applications.
- **Roadmap:**
  - Preliminary optical & radio data are in-hand.
  - Increase number of sources in common between optical and radio
  - Expect to be limited by systematic calibration errors
  - Quantify and reducing systematics by
    - getting data in three radio bands (8, 24, 32 GHz)
    - Compare independent analysis chains
    - Image sources in radio to quantify non-pointlike structure
- **Preliminary results: Gaia DR1-aux vs. VLBI**
  - Excellent 3-D tie precision of  $\sim 20 \mu\text{as}$ .
  - Random scatter  $\sim 400$  to  $500 \mu\text{as}$  limited by Gaia statistical error
  - Accuracy limited by systematic errors at  $100 - 500 \mu\text{as}$ .
  - SX (8 GHz) on low end  $\sim 100 \mu\text{as}$ . K (24) Ka (32) 200-500  $\mu\text{as}$ .
  - Hints that 24 and 32 GHz VLBI are cleaner than 8 GHz
  - K and Ka lower percentage outliers, smaller scatter vs Gaia
  - Control of VLBI systematics will require increased southern observations.



Gaia Optical